

1 **Changes of the tropical tropopause layer under global warming**

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ABSTRACT

9 We investigate changes in the tropical tropopause layer (TTL) in response
10 to carbon dioxide increase and surface warming separately in an atmospheric
11 general circulation model, and find that both effects lead to a warmer tropical
12 tropopause. Surface warming also results in an upward shift of the tropopause.
13 We perform a detailed heat budget analysis to quantify the contributions from
14 different radiative and dynamic processes to changes in the TTL temperature.
15 When carbon dioxide increases with fixed surface temperature, a warmer TTL
16 mainly results from the direct radiative effect of carbon dioxide increase. With
17 surface warming, the largest contribution to the TTL warming comes from the
18 radiative effect of the warmer troposphere, which is partly canceled by the ra-
19 diative effect of the moistening at the TTL. Strengthening of the stratospheric
20 circulation following surface warming cools the lower stratosphere dynami-
21 cally and radiatively via changes in ozone. These two effects are of compa-
22 rable magnitudes. This circulation change is the main cause of temperature
23 changes near 63 hPa, but is weak near 100 hPa. Contributions from changes in
24 convection and clouds are also quantified. These results illustrate the heat bud-
25 get analysis as a useful tool to disentangle the radiative-dynamical-chemical-
26 convective coupling at the TTL and to facilitate an understanding of inter-
27 model difference.

28 **1. Introduction**

29 The tropical tropopause layer (TTL) is the transition region between the troposphere and the
30 stratosphere (Fueglistaler et al. 2009; Randel and Jensen 2013). As one moves from the tro-
31 posphere into the stratosphere, static stability sharply increases, convective activities and clouds
32 evanesce, radiative heating rates change from net cooling to net warming, and the meridional
33 circulation shifts from the Hadley circulation into the much wider Brewer-Dobson circulation.
34 Many chemically and/or radiatively important species, including water vapor and ozone, experi-
35 ence sharp gradients in their concentrations across the TTL. The TTL affects both the troposphere
36 and the stratosphere and exerts influences well beyond the tropical region. The thermal structure
37 of the TTL is of particular interest as it sets the stratospheric water vapor concentration (Mote et al.
38 1996), changes of which may have contributed to the recent hiatus of surface warming (Solomon
39 et al. 2010). It also affects the climate system through changes of clouds, especially cirrus clouds
40 (Li and Thompson 2013; Virts et al. 2010). Recent studies also suggested a possible link between
41 the TTL temperature and the intensity of tropical cyclones (Emanuel et al. 2013; Wang et al. 2014).

42 The thermal structure of the TTL is an emergent property of the complex coupling among con-
43 vection, radiation, and circulations of various scales (Fueglistaler et al. 2009; Randel and Jensen
44 2013, and references therein). It can be altered by climate change in multiple ways, which involve
45 changes in temperature outside the TTL, concentrations of water vapor, ozone and greenhouse
46 gases (GHGs), cloud properties, circulation patterns and convective activities. Given the subtle
47 nature of the balance among all these factors, it might be surprising that almost all general cir-
48 culation models (GCMs) and chemistry climate models (CCMs) predict a warming and upward-
49 shifting trend of the tropical tropopause over the 21st century (Gettelman et al. 2010; Kim et al.
50 2013).

51 Shepherd (2002) proposed a conceptual model to explain the tropopause change, which pos-
52 tulates a warmer and higher tropopause when the troposphere warms, but a colder and higher
53 tropopause when the stratosphere cools (both of which would occur as GHGs increases). This re-
54 lationship has been confirmed with observations (Seidel and Randel 2006) and simulations (San-
55 ter et al. 2003). Based on linear regression analysis, Austin and Reichler (2008) attributed the
56 tropopause changes from 1960 to 2100 to changes in the Brewer-Dobson circulation, stratospheric
57 ozone and sea surface temperatures (SSTs). However, due to the highly coupled nature of the TTL
58 processes, it is hard to avoid ambiguity in regression-based attribution analyses. Previous mech-
59 anistic studies investigated the radiative balance of the TTL and its sensitivity to changes in the
60 radiatively active species (Thuburn and Craig 2002; Gettelman et al. 2004). These radiative trans-
61 fer calculations were, however, done in a relatively simplistic fashion, and the coupling between
62 the species and circulation was largely neglected.

63 In this paper, we seek a more complete understanding of the simulated warming trends at the
64 TTL as GHGs increases. By analyzing the heat budget at the TTL, we disentangle the coupled
65 radiative, dynamic and thermodynamic processes and quantify the contribution from each pro-
66 cess. The organization of the paper is as follows. Section 2 describes the experiment setup and
67 the methodology for the heat budget analysis. The main results are presented in Section 3. A
68 discussion on the robustness of the results is given in Section 4, which is followed by a summary
69 and conclusion in Section 5.

70 **2. Methodology**

71 *a. model simulations*

72 We conduct three pairs of idealized perturbation experiments using the Geophysical Fluid Dy-
73 namics Laboratory (GFDL) atmospheric model AM3 (Donner et al. 2011), the atmospheric com-
74 ponent of the GFDL coupled climate model (CM3). This model has 48 vertical layers with a
75 model top at 0.01 hPa (~ 86 km), of which 7 layers are between 40 hPa and 200 hPa. Note that
76 AM3 incorporates an interactive chemistry scheme in both the stratosphere and troposphere, thus
77 allowing ozone to be transported by circulation and to adjust to the corresponding climate. Ba-
78 sic simulation characteristics of this model are documented in Donner et al. (2011). We specify
79 the sea surface temperatures (SSTs) and the concentration of carbon dioxide (CO_2) in the experi-
80 ments. As the first perturbation, we quadruple the CO_2 concentration from 368 ppm in the control
81 experiment to 1472 ppm (4x CO_2). As the second perturbation, we uniformly increase SST by 4
82 K from the present-day climatology in the control (4KSST). As the third perturbation, we apply
83 both quadrupling CO_2 and 4K increase of SST (COMBINE). All other external forcings remain
84 the same. Each simulation is run for 11 model years, and we analyze the last 10 years. All results
85 are averaged over the tropics ($20^\circ\text{S} - 20^\circ\text{N}$). Zonal mean temperature and zonal wind changes in
86 these experiments are shown in the supplementary materials.

87 *b. heat budget analysis*

88 The thermodynamic equation of the atmosphere can be written as:

$$\frac{\partial \theta}{\partial t} = Q_{dyn} + Q_{conv} + Q_{rad} \quad (1)$$

89 in which Q_{dyn} , Q_{conv} and Q_{rad} represent potential temperature (θ) tendency driven by advection,
90 phase change of water and radiation, respectively. In a quasi-equilibrium climate state, Q_{dyn} ,
91 Q_{conv} and Q_{rad} effectively balance each other out, resulting in $\partial\theta/\partial t = 0$. Now considering the
92 difference between two climate states, we will have:

$$\Delta Q_{dyn} + \Delta Q_{conv} + \Delta Q_{rad} = 0 \quad (2)$$

93 We further decompose ΔQ_{rad} into terms due to different controlling factors:

$$\begin{aligned} \Delta Q_{rad} &= \frac{\partial Q_{rad}}{\partial T_{loc}} \Delta T_{loc} + \sum_i \frac{\partial Q_{rad}}{\partial X_i} \Delta X_i \\ &= \Delta Q_{rad, T_{loc}} + \sum_i \Delta Q_{rad, X_i}, \end{aligned} \quad (3)$$

94 in which T_{loc} is the temperature at the location of interest, X_i includes concentrations of radiatively
95 active species (such as ozone, water vapor, GHGs), clouds, and non-local temperature. Changes
96 in these species and clouds may be caused by variations in large-scale circulation or convection.
97 Then Eq. (2) can be written as:

$$-\Delta Q_{rad, T_{loc}} = \Delta Q_{dyn} + \Delta Q_{conv} + \sum_i \Delta Q_{rad, X_i} \quad (4)$$

98 Note that in the much simplified Newtonian cooling framework, the left hand side of the above
99 equation would correspond to $\frac{\Delta T_{loc}}{\tau}$, where τ is the radiative relaxation time, which is ~ 30 days
100 in the TTL (Hartmann et al. 2001). When an atmosphere layer becomes warmer, it will emit more
101 longwave radiation. In order to sustain the warming, there must be additional heating from either
102 dynamical, convective or other radiative processes to balance the increased longwave emission.
103 Equation (4) helps quantify the contributions of different physical processes to the changes in the
104 TTL temperature.

105 *c. estimation of heating rates*

106 Q_{dyn} , Q_{conv} and Q_{rad} are readily archived in the model output. Since Q_{dyn} is largely brought
 107 about by the vertical transport of the Brewer-Dobson circulation in the TTL region, it can be
 108 approximated by $-\bar{\theta}_z \bar{w}^*$, in which $\bar{\theta}_z$ is the vertical derivative of zonal mean potential temperature,
 109 and \bar{w}^* is the Transformed Eulerian Mean (TEM) vertical velocity (Rosenlof 1995; Yang et al.
 110 2008). We also calculate $\bar{\theta}_z$ and \bar{w}^* from other model outputs to further decompose the total
 111 ΔQ_{dyn} into those caused by $\Delta \bar{\theta}_z$ and $\Delta \bar{w}^*$.

112 To estimate the individual radiative heating rates, we employ the off-line version of the radiative
 113 transfer model used in AM3 (Freidenreich and Ramaswamy 1999; Schwarzkopf and Ramaswamy
 114 1999; GFDL Global Atmospheric Model Development Team 2004). The radiative heating rate
 115 change due to each perturbation $\Delta Q_{rad, X_i}$ is calculated using the partial radiative perturbation
 116 method (Wetherald and Manabe 1988). ($\Delta Q_{rad, T_{loc}}$ is computed in the same way as $\Delta Q_{rad, X_i}$).
 117 We perform a two-sided perturbation to minimize the influence of the decorrelation perturbation
 118 (Colman and McAvaney 1997; Soden et al. 2008), i.e.,

$$\Delta Q_{rad, X_i} = \frac{1}{2} [Q_{rad}(X_i^P, X_{j \neq i}^C) - Q_{rad}(X_i^C, X_{j \neq i}^C) + Q_{rad}(X_i^P, X_{j \neq i}^P) - Q_{rad}(X_i^C, X_{j \neq i}^P)] \quad (5)$$

119 in which X^C and X^P stand for radiation-relevant variables from the control simulation, and from the
 120 perturbed simulation, respectively. The off-line radiative transfer is performed every three hours at
 121 each model grid using the instantaneous temperature, water vapor, ozone and cloud fields archived
 122 from the GCM simulations. To reduce computational cost, we construct a synthetic one-year
 123 timeseries by randomly sampling the entire ten-year simulation. The averaged radiative heating
 124 rates calculated from these one-year profiles are very close to the ten-year averages. The clouds in
 125 AM3 are either explicitly resolved or parameterized by shallow and deep cumulus schemes. Both

126 types are seen by radiation. Cloud overlap is treated using the Monte Carlo independent column
127 approximation (Pincus et al. 2003). The cloud droplet size is calculated from the prognostic cloud
128 water content and droplet number concentration. The cloud ice particle size is parameterized as a
129 function of temperature. More detail can be found in Donner et al. (2011).

130 For perturbations in temperature and water vapor, instead of perturbing the whole profile at once,
131 we perturb the tropospheric, TTL and stratospheric part separately, as the governing physics vary
132 for these regions. We defined the tropospheric region as the model layers below the level of zero
133 net clear-sky radiative heating (LZRH), the stratospheric region as the model layers above the cold-
134 point tropopause, and the TTL as the layers between. For the control and perturbed simulations, we
135 calculated the pressure of the cold-point tropopause from the tropical mean climatology, and use
136 the lower of these two values as the TTL top boundary. Similarly to define the bottom boundary,
137 we use the highest pressure LZRH of the two simulations.

138 **3. Results**

139 Fig. 1 shows the tropical-averaged temperature profiles in our simulations. We also mark the
140 tropopause levels based on different definitions: the LZRH, the World Meteorological Organiza-
141 tion (WMO) defined tropopause where the lapse rate equals 2 K/km, and the cold-point tropopause
142 where the lapse rate is zero. It is clear from Fig. 1 that the tropical tropopause warms significantly
143 in both experiments. In the 4xCO₂ case, the troposphere warms slightly, and the strongest warm-
144 ing is located around 90 hPa. The tropics cools above ~ 70 hPa, and the strongest cooling occurs
145 roughly at the stratopause. The cold-point tropopause remains at ~ 90 hPa level, and warms by
146 0.8 K. In the 4KSST case, the tropics warms below ~ 80 hPa and cools above. The strongest
147 warming is located in the upper troposphere around 200 hPa, and the strongest cooling is in the
148 lower stratosphere around 60 hPa. The cold-point tropopause is lifted from 90 hPa to 77 hPa,

149 and the cold-point temperature warms by 1.4 K. In the COMBINE case in which CO₂ and SST
150 changes simultaneously, the resulted temperature change profile matches with the sum of those
151 from 4xCO₂ and 4KSST perturbations, with the cold-point temperature warmed by 2.2K. This is
152 in agreement with previous studies by Kodama et al. (2007) and Kawatani et al. (2012) who also
153 found negligible nonlinearity in stratospheric circulation responses to both CO₂ and SST increase.

154 Note that on average, the CMIP5 models under RCP8.5 predict a cold-point tropopause warming
155 of ~ 1.5 K (Kim et al. 2013). Gettelman et al. (2010) showed that most chemistry climate models
156 simulate a 0.5 – 1.0 K warming of the cold point over the 21st century. Given a typical tropical
157 cold point temperature of 190 K, a 1 K warming at the cold-point would lead to $\sim 18\%$ or 0.6
158 ppmv increase of stratospheric water vapor concentration, assuming that the stratospheric water
159 vapor concentration is equal to saturation concentration at the cold-point.

160 Compared to simulations with more realistic forcings, these idealized experiments provide a
161 relatively clean setting to explore the TTL changes. At the same time, the fully interactive ozone,
162 water vapor and clouds in this model make it possible to study a full range of responsible physical
163 processes, and to assess their relative contributions. We focus on the 4xCO₂ and 4KSST cases in
164 the following text since the COMBINE case can be largely explained by the sum of the two. Also
165 note that these two cases represent changes occurring at different time scales. Adjustments of the
166 climate system to CO₂ increase that are independent from surface temperature changes would be
167 much faster than those mediated by changes in surface temperature (Sherwood et al. 2015).

168 *a. 4xCO₂ case*

169 Figure 2 illustrates changes of some key parameters in this experiment. With quadrupling CO₂,
170 the middle and upper stratosphere radiatively cool up to 17 K, which is in agreement with many
171 previous studies (e.g., Manabe and Wetherald 1967; Fels et al. 1980; Ramaswamy et al. 1996;

172 Shine et al. 2003). The troposphere warms ~ 0.3 K following the warming of the land. Water vapor
173 concentration increases by a few percent in the troposphere, while the relative humidity decreases
174 by $\sim 0.5\%$ near 100 hPa and 700 hPa and increases in the middle troposphere. What is less
175 recognized by previous studies is the ~ 0.8 K warming at the cold-point tropopause. Stratospheric
176 water vapor concentration increases as the tropopause warms. The moistening amounts to 14%
177 just above the cold point, and reduces to a few percent in the upper stratosphere. The increase
178 of the relative humidity peaks at $\sim 3\%$ in the lower stratosphere. Tropical upwelling from the
179 Brewer-Dobson circulation enhances with the increase of CO_2 , consistent with previous studies
180 (Oman et al. 2009; Kodama et al. 2007). The acceleration is stronger in the upper stratosphere
181 than elsewhere. More interestingly, the upwelling at the tropopause also increased. This increased
182 upwelling across the tropopause dilutes lower stratospheric ozone. In contrast, ozone increases
183 in the middle and upper stratosphere, mainly due to a slower photochemical destruction at colder
184 temperature (Barnett et al. 1975). The model also simulates a small increase of ozone below 100
185 hPa. Consistent with changes in the relative humidity, clouds decreases at the tropopause and in
186 the lower troposphere. The reduction of low level clouds in response to CO_2 increase has been
187 reported by many previous studies (e.g., Andrews and Forster 2008; Colman and McAvaney 2011;
188 Zelinka et al. 2013), while less attention has been paid to changes of clouds near the tropopause.

189 All the changes discussed above may potentially influence the heat budget at the TTL. Their
190 contributions are depicted in Figs. 3 and 4. As shown in Fig. 3, the longwave cooling arising
191 from the warmer tropopause is balanced almost entirely by $\sum_i \Delta Q_{rad, X_i}$ in the 4x CO_2 case, with
192 negligible contributions from ΔQ_{dyn} and ΔQ_{conv} . It is clear from Fig. 4 that the warming at
193 100 hPa is driven mostly by the direct radiative effect of higher CO_2 concentration. As shown
194 in Thuburn and Craig (2002), this radiative heating from CO_2 exists due to the strong curvature
195 of the temperature profile near the tropopause. Since longwave emission is proportional to the

196 fourth power of the temperature at which it occurs, the cold tropopause implies that the radiative
197 flux emitted from the tropopause would be smaller than that from layers above and below. When
198 CO₂ increases, the stronger absorption of radiative fluxes at the tropopause from atmospheric
199 layers above and below exceeds the stronger emission from the tropopause. Hence a net longwave
200 heating arises there. CO₂ also absorbs at a few shortwave bands (e.g., Liou 2002). The absorption
201 at these shortwave bands contributes to the radiative heating at the TTL as well. The radiative
202 warming from CO₂ increase is also reported by McLandress et al. (2014).

203 The colder stratosphere, which also results from increased CO₂ (e.g., Manabe and Wetherald
204 1967; Shine et al. 2003), tends to cool the tropopause radiatively. The enhanced upwelling across
205 the tropopause produces a dynamical cooling. The radiative effects of the changes in tropospheric
206 temperature, ozone, water vapor and clouds are much smaller than the direct radiative heating
207 from CO₂. The fact that the summation of individual heating rates agrees well with the estimation
208 obtained by subtracting $\Delta Q_{rad, T_{loc}}$ from model-diagnosed ΔQ_{rad} serves as a validation of our off-
209 line radiative transfer calculations (Fig. 4(b)).

210 *b. 4KSST case*

211 The changes of some key variables are shown in Fig. 5. Compared to the 4xCO₂ experiment,
212 dynamics and convection play more important roles in the 4KSST experiment (Fig. 6). The
213 composition of the heat budget varies with height. We choose to focus on two levels, 63 hPa and
214 100 hPa, since opposite temperature changes are seen at them. The detailed heat budgets are given
215 in Fig. 7.

216 The tropical troposphere follows the moist adiabatic lapse rate. As a result, the troposphere
217 warms more than the surface (Fig. 5), and tends to warm the atmospheric layers above by emitting
218 more longwave radiation. This effect counts for the strongest warming tendency at 100 hPa (Fig.

219 7 (b)), but is relatively weak at 63 hPa (Fig. 7 (a)). The tropospheric warming is accompanied by
220 moistening, which causes a weak radiative cooling at both levels.

221 The Brewer-Dobson circulation is expected to strengthen in a warmer climate (e.g., Butchart
222 2014; Lin et al. 2015). This is confirmed by the stronger vertical velocity (Fig. 5). The enhanced
223 upwelling would have a tendency to cool the atmosphere adiabatically. It is, however, important
224 to note that this dynamic cooling is mediated by changes in the static stability (Fueglistaler et al.
225 2011). In the 4KSST experiment, the tropopause shifts upwards and the static stability decreases
226 near the original tropopause. The effect of decreased static stability dominates that of stronger
227 upwelling at 100 hPa, resulting in a weakly positive heating rate. This is in contrast to ΔQ_{dyn} being
228 the largest cooling term at 63 hPa. The stronger Brewer-Dobson circulation also transports more
229 tropospheric air into the stratosphere and dilutes the ozone concentration in the lower stratosphere.
230 The radiative effect from the decreased ozone is the second largest cooling term at 63 hPa, but is
231 negligible at 100 hPa. The colder stratosphere has a cooling effect on the tropopause.

232 As the lower stratosphere cools and the upper troposphere warms, the tropopause shifts upwards,
233 allowing convection to penetrate deeper and clouds to form at higher levels. The upward shift of
234 clouds in response to surface warming is a robust feedback mechanism (Hartmann and Larson
235 2002; Zelinka and Hartmann 2010). The latent heat release from the deeper convection and the
236 radiative effect of cloud changes each contribute about a fifth of the heating that is needed for
237 sustaining the warming at 100 hPa. Their effects are negligible at 63 hPa since most convection
238 and clouds are confined below. Water vapor concentration increases by about 50% in the lower
239 stratosphere due to a warmer cold-point as well as stronger convection overshoot. At 100 hPa, the
240 moistening of the TTL causes the strongest cooling, but the stratospheric moistening leads to a
241 weak warming. Neither has any appreciable impact on the temperature change at 63 hPa.

242 Since the tropopause has been lifted considerably in this case, the above analysis on the fixed
243 pressure levels cannot answer the question of what causes the warming at the tropopause. To
244 answer this question, we repeat the above analysis in the coordinate of relative height to the WMO
245 tropopause (Birner et al. 2002; Pan et al. 2004). We first identify the WMO tropopause from the
246 temperature profile at each grid and time step. We then shift the profiles of all radiation-relevant
247 variables at this grid and time step by $\Delta z = -H \ln(P_{TP}/P_{ref})$, where H is the scale height, P_{TP} is
248 the WMO tropopause pressure, and $P_{ref} = 100 \text{ hPa}$. These shifted profiles are then used for the
249 off-line radiative transfer calculation. The model-diagnosed daily heating rates are converted to the
250 tropopause-relative coordinate in the same way. Note that the conversion between the coordinates
251 leads to deviations of the off-line radiative calculations from the model-diagnosed one, and hence
252 the resulted heat budget in this case is not fully closed.

253 Figure 8 shows the radiative and dynamical properties in the tropopause-relative coordinate.
254 Similar to what is shown in the original log pressure coordinate, water vapor increases in both the
255 stratosphere and troposphere, clouds shift upwards, and the upward transport enhanced in the TTL
256 region (though with smaller magnitudes). However, changes in temperature and ozone are differ-
257 ent in the tropopause-relative coordinate compared to the pressure coordinate. Here warming is
258 seen not only in the troposphere but also in the lower stratosphere. Ozone concentration increases
259 rather than decreases in the lower stratosphere.

260 The heat budget at the composited tropopause is shown in Fig. 9. As shown in the figure,
261 changes in temperature, ozone, clouds and convection all leads to a warmer tropopause, with
262 the largest contribution coming from the warmer troposphere. The tropopause is cooled by the
263 stronger upwelling as well as moistening in the troposphere and at the tropopause. The largest
264 cooling effect comes from the moistening at the tropopause. The two estimates of $\sum \Delta Q_{rad, X_i}$
265 differ by about 15%.

266 4. Discussion

267 Our heat budget analysis suggests that the radiative effect from tropospheric warming and the
268 direct radiative effect from CO₂ increase are the two largest contributing factors to the tropopause
269 warming. They are countered mainly by the strengthening of the stratospheric circulation and the
270 moistening near the tropopause. But the magnitudes of the cooling from circulation changes and
271 moistening are in general weak at the tropopause. This may explain why most models show a
272 warmer tropopause under global warming. In practice, the magnitudes of the tropopause warming
273 vary vastly from model to model (Gettelman et al. 2010; Kim et al. 2013). The heat budget
274 analysis shown here would be useful for identifying the sources of inter-model spreads. We leave
275 a quantitative assessment of the inter-model spread to future work, but offer a qualitative discussion
276 below.

277 The direct radiative warming at the tropopause from increased CO₂ varies with both the CO₂
278 base value as well as details of the radiative transfer model. Figure 10 shows the increases in
279 longwave and shortwave heating rates at the tropopause as CO₂ concentration increases from 200
280 ppm to 1600 ppm. These heating rates are calculated using AM3's radiative transfer codes; two
281 more sophisticated radiative transfer models: Fu-Liou (Fu and Liou 1992) and the Rapid Radiative
282 Transfer Model (RRTM, Mlawer et al. 1997; Clough et al. 2005); as well as the Reference Forward
283 Model (RFM, Dudhia 2005) line-by-line code, which is the most accurate. The calculation is done
284 for the tropical-averaged profiles at the equinox from the control experiment. Only clear-sky and
285 aerosol-free results are shown. The shortwave heating rate varies roughly linearly with logarithmic
286 increase of CO₂. Different radiative transfer models agree relatively well for the shortwave heating
287 rate change. The longwave part, on the other hand, shows less warming or even cooling when
288 CO₂ increases from a high base value. Diverse responses in longwave heating rate are seen among

289 different radiative transfer models when the CO₂ concentration is higher than 600 ppm. Even for a
290 moderate CO₂ increase from 400 ppm to 600 ppm, the difference in longwave heating rate increase
291 at the tropopause among radiative transfer models is greater than 40%. Note that the long radiative
292 relaxation time near the tropopause (Fels 1982; Ramaswamy and Ramanathan 1989; Thuburn
293 and Craig 2002; Hartmann and Larson 2002; Gettelman et al. 2004) implies a large temperature
294 response to any change in the heating rate. Therefore, an error in the heating rate of similar
295 magnitude would then translate into a larger error in temperature at the tropopause than at other
296 levels.

297 The radiative warming at the tropopause from the warmer troposphere is largely determined
298 by temperature change at the tropical upper troposphere. While the tropical upper tropospheric
299 warming is a robust feature of the global warming simulated virtually by all models (Ramaswamy
300 et al. 2006), recent studies show that the magnitudes of the warming differ by more than threefolds
301 among CMIP3 and CMIP5 models (Fu et al. 2011; Po-Chedley and Fu 2012). This large inter-
302 model spread may be attributed to the large uncertainty in the cumulus parameterization as well as
303 the dependence on the detailed sea surface temperature patterns (Flannaghan et al. 2014). Lin and
304 Fu (2013) further show that the acceleration of the stratospheric circulation is also tightly coupled
305 to the warming at the tropical upper troposphere. Note that about half of the influence from strato-
306 spheric circulation change is realized through changing ozone concentration. This mechanism will
307 be absent in many CMIP3 and CMIP5 models with prescribed ozone.

308 While in general there is uncertainty regarding cloud properties and their effects in models, con-
309 vection and clouds play relatively minor roles in altering tropopause temperature in this model.
310 Previous studies suggest that the upward shift of clouds is a robust response to global warming
311 (Hartmann and Larson 2002; Zelinka and Hartmann 2010). This, however, does not necessar-
312 ily translate to a robust change at the tropopause. If convection and cloud tops are well below

313 the tropopause, any shift in convection or clouds would pose negligible effect on the tropopause.
314 Thuburn and Craig (2002) showed that the radiation from the $15 \mu\text{m}$ CO_2 band plays an important
315 role in separating the cold-point tropopause and the convection top. This, again, suggests the im-
316 portance to improve the accuracy of radiative transfer calculations, especially near the tropopause
317 region.

318 **5. Summary and conclusions**

319 Change in the tropical tropopause is an important consequence of the GHG-induced global cli-
320 mate change. Here we investigate the tropical tropopause change in response to a quadrupling CO_2
321 with fixed SST and a uniform SST warming of 4K with GFDL AM3. The tropopause becomes
322 warmer in both experiments. The tropopause height (pressure) shifts upwards following surface
323 warming, but remains unchanged as CO_2 increases.

324 We perform a detailed heat budget analysis at the tropopause to distinguish and quantify the con-
325 tributions from different radiative and dynamic processes to the tropopause temperature change.
326 The heat budget analysis shows that in the $4\times\text{CO}_2$ experiment, the tropopause warming is mainly
327 caused by the direct radiative effect from CO_2 increase. In the 4KSST experiment, the largest con-
328 tributor at 100 hPa is the radiative warming from a warmer troposphere. The temperature change
329 at 63 hPa, on the other hand, is dominated by cooling induced by a stronger Brewer-Dobson
330 circulation, both dynamically and radiatively via changing ozone. Taking the tropopause height
331 change into account, we redo the heat budget analysis in the tropopause-relative coordinate for the
332 4KSST experiment. The composite heat budget reveals that changes in tropospheric and strato-
333 spheric temperature, moistening in the stratosphere, changes in ozone, convections and clouds all
334 lead to a warming of the tropopause, with the warmer troposphere being the largest contributor.
335 The tropopause is cooled by stronger upwelling across the tropopause and the moistening in the

336 troposphere and at the tropopause, among which the wetter tropopause contributes the most. We
337 substantiate that the radiative warming at the tropopause from CO₂ increase and the warmer tro-
338 posphere are the dominant contributors to tropical tropopause change under global warming, and
339 that inter-model differences may be traced back to a number of key processes (such as radiative
340 transfer scheme, the tropical upper tropospheric warming, ozone transport and the convection top
341 climatology.)

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498 **LIST OF FIGURES**

499 **Fig. 1.** (a) Tropical mean temperature profiles in the control (solid) and 4xCO2 (dashed) experi-
500 ments. The horizontal bars mark the tropopauses based on different definitions. From bot-
501 tom to top are the LZRH tropopause, the WMO tropopause and the cold-point tropopause.
502 (b) Tropical mean profile of temperature difference for 4xCO2. Gray shading plots the 95%
503 confidence interval based on the Student’s t-test. (c) and (d), as in (a) and (b), except for
504 4KSST. (e) and (f), as in (a) and (b), except for COMBINE. Blue line in (f) plots the sum of
505 temperature change from 4xCO2 and 4KSST experiments. 26

506 **Fig. 2.** Tropical mean profiles of (a) temperature, (b) specific humidity, (c) relative humidity, (d)
507 ozone concentration, (e) cloud fraction, and (f) the Transformed Eulerian mean (TEM) ver-
508 tical velocity. Black solid lines are from the control simulation, dashed lines are from the
509 perturbed simulation, red lines are the difference between the control and 4xCO2 experi-
510 ments, and the blue lines show the relative difference. The gray shading indicates the 100-
511 hPa layer for which a detailed heat budget analysis is performed. The horizontal lines mark
512 the boundaries separating the stratosphere, the tropopause layer and the troposphere. 27

513 **Fig. 3.** Profiles of heating rate changes in the upper troposphere/lower stratosphere for 4xCO2.
514 Markers indicate the centers of model layers. The horizontal bars mark the tropopauses
515 based on different definitions as in Fig. 1. 28

516 **Fig. 4.** (a) The radiative cooling from 100-hPa temperature changes ($-\Delta Q_{rad,Tloc}$), and heating
517 rates changes due to advection (ΔQ_{dyn}), latent heat release (ΔQ_{conv}), and radiative perturba-
518 tions ($\Delta Q_{rad,X_i}$) at 100 hPa for 4xCO2. The radiative perturbations include temperature and
519 water vapor changes in the troposphere (T), the TTL (TP) and the stratosphere (S), changes
520 in ozone concentration (O3), clouds (CLD) and carbon dioxide concentration (CO2). (b)
521 Heating rate changes from all radiative perturbations estimated by summing each individual
522 perturbations from the off-line calculations (left) and by subtracting $\Delta Q_{rad,Tloc}$ from module-
523 diagnosed ΔQ_{rad} (right). See text for more explanation. 29

524 **Fig. 5.** As in Fig. 2, except for 4KSST. 30

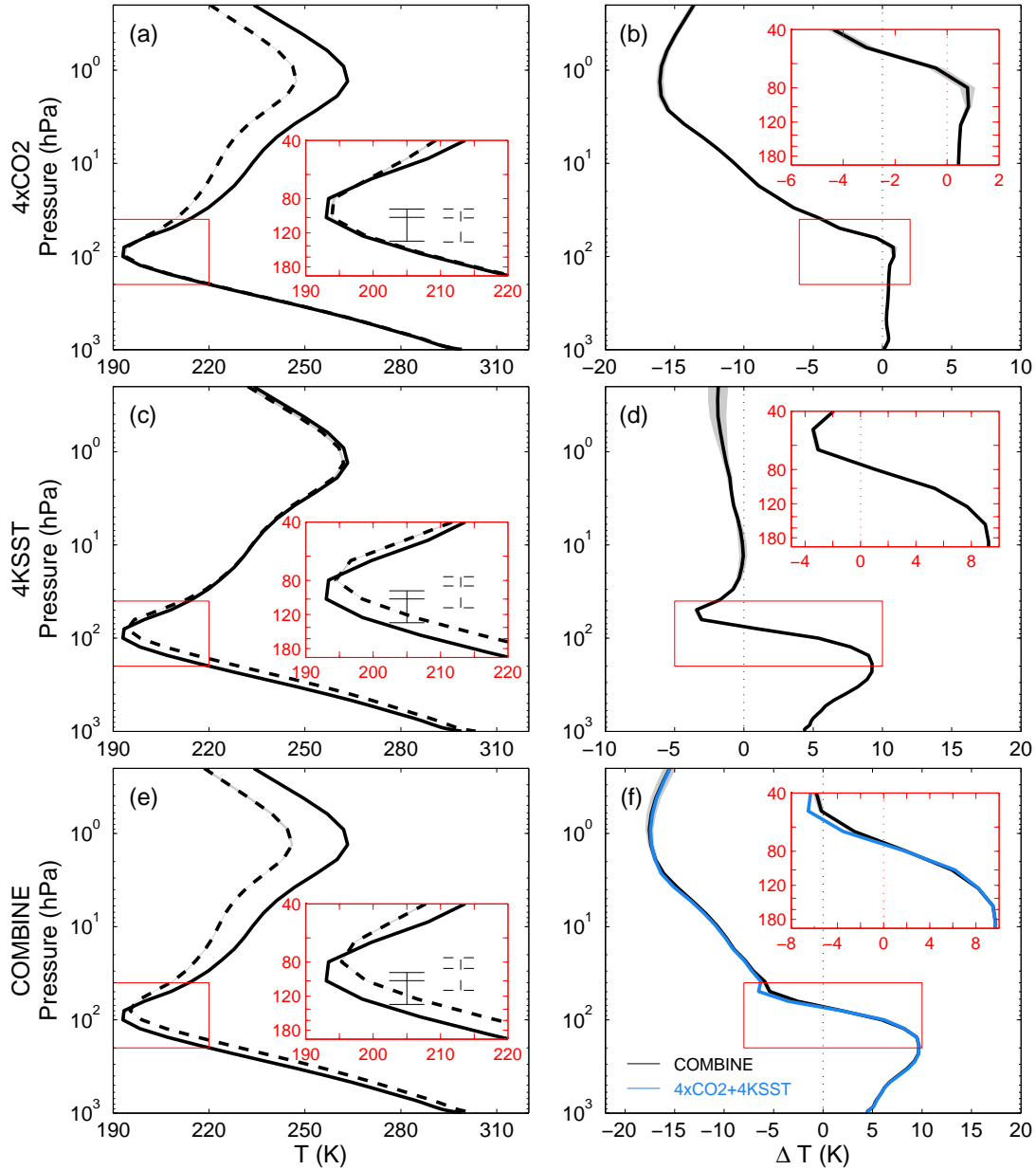
525 **Fig. 6.** As in Fig. 3, except for 4KSST. 31

526 **Fig. 7.** As in Fig. 4, except for (a) the 63-hPa layer and (b) the 100-hPa layer for 4KSST. 32

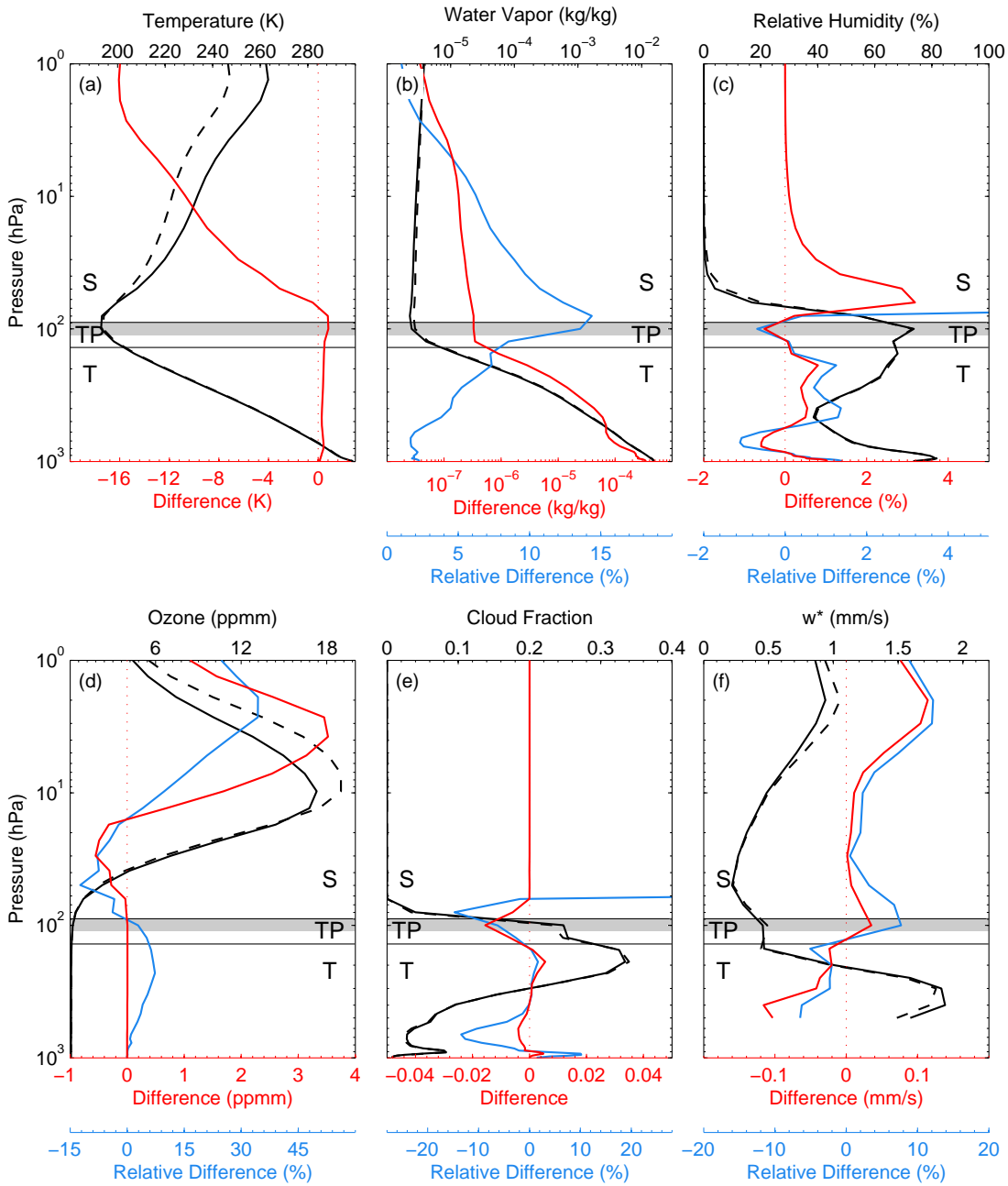
527 **Fig. 8.** As in Fig. 5, except for in the tropopause-relative coordinate. The gray shading indicates
528 the 100-hPa layer where the composite tropopause is located. 33

529 **Fig. 9.** As in Fig. 7, except for the composite tropopause. 34

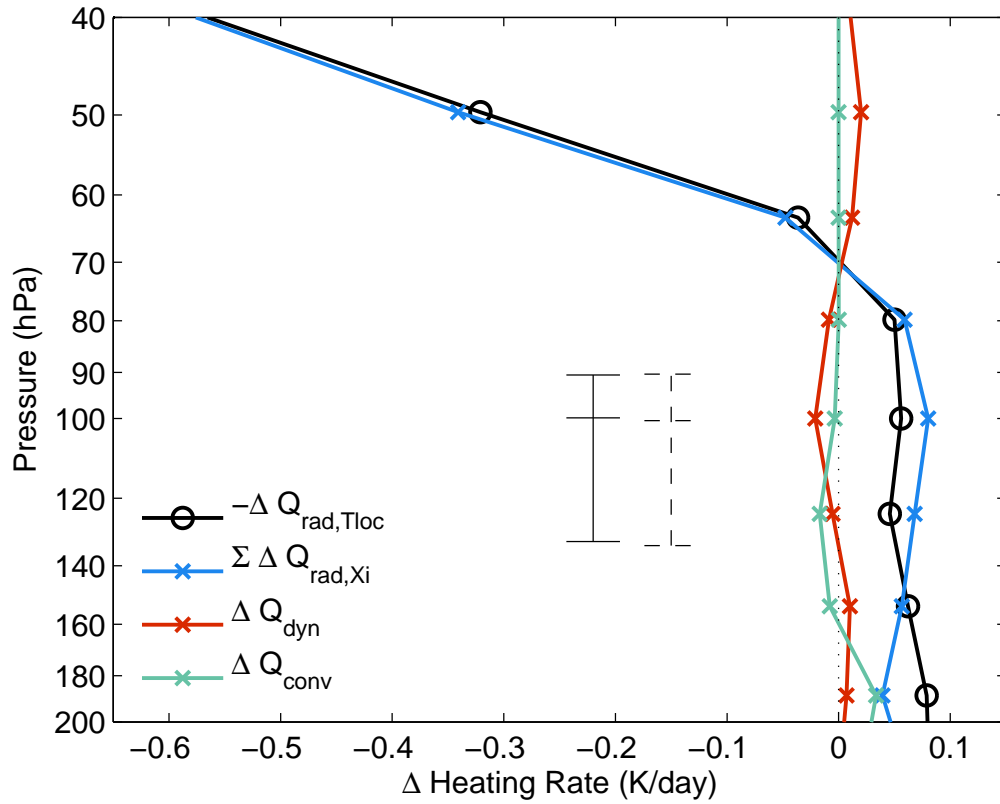
530 **Fig. 10.** Longwave (blue) and shortwave (red) heating rate changes at the tropopause as carbon diox-
531 ide concentration increases from 200 ppm. The heating rates are calculated using AM3
532 radiative transfer code (triangle), Fu-Liou radiative transfer code (cross), the RRTM (cir-
533 cle) and the RFM line-by-line code (square). The radiative calculations are done using the
534 tropical mean profiles from the control simulation, and are carried out at the equinox under
535 clear-sky aerosol-free conditions. See text for more explanation. 35



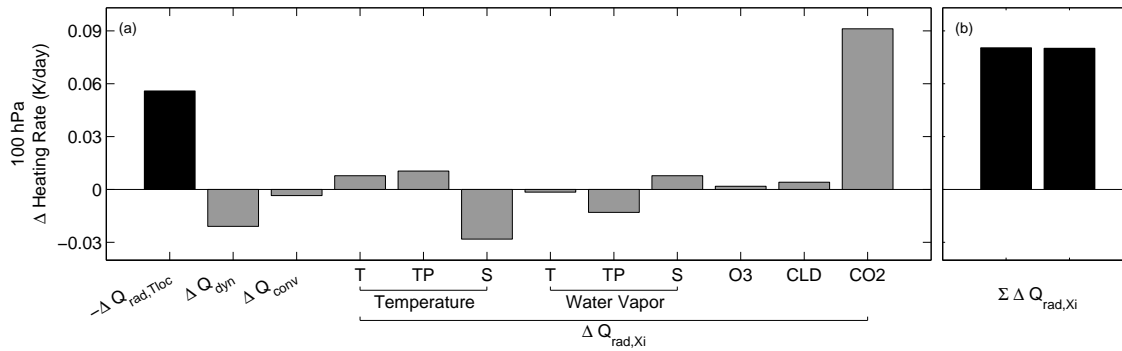
536 FIG. 1. (a) Tropical mean temperature profiles in the control (solid) and 4xCO₂ (dashed) experiments.
 537 The horizontal bars mark the tropopauses based on different definitions. From bottom to top are the LZRH
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 540 in (a) and (b), except for 4KSST. (e) and (f), as in (a) and (b), except for COMBINE. Blue line in (f) plots the
 541 sum of temperature change from 4xCO₂ and 4KSST experiments.



542 FIG. 2. Tropical mean profiles of (a) temperature, (b) specific humidity, (c) relative humidity, (d) ozone
 543 concentration, (e) cloud fraction, and (f) the Transformed Eulerian mean (TEM) vertical velocity. Black solid
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 546 indicates the 100-hPa layer for which a detailed heat budget analysis is performed. The horizontal lines mark
 547 the boundaries separating the stratosphere, the tropopause layer and the troposphere.



548 FIG. 3. Profiles of heating rate changes in the upper troposphere/lower stratosphere for 4xCO2. Markers
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 550 in Fig. 1.



551 FIG. 4. (a) The radiative cooling from 100-hPa temperature changes ($-\Delta Q_{rad,Tloc}$), and heating rates changes
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 553 4xCO₂. The radiative perturbations include temperature and water vapor changes in the troposphere (T), the
 554 TTL (TP) and the stratosphere (S), changes in ozone concentration (O₃), clouds (CLD) and carbon dioxide con-
 555 centration (CO₂). (b) Heating rate changes from all radiative perturbations estimated by summing each individual
 556 perturbations from the off-line calculations (left) and by subtracting $\Delta Q_{rad,Tloc}$ from module-diagnosed ΔQ_{rad}
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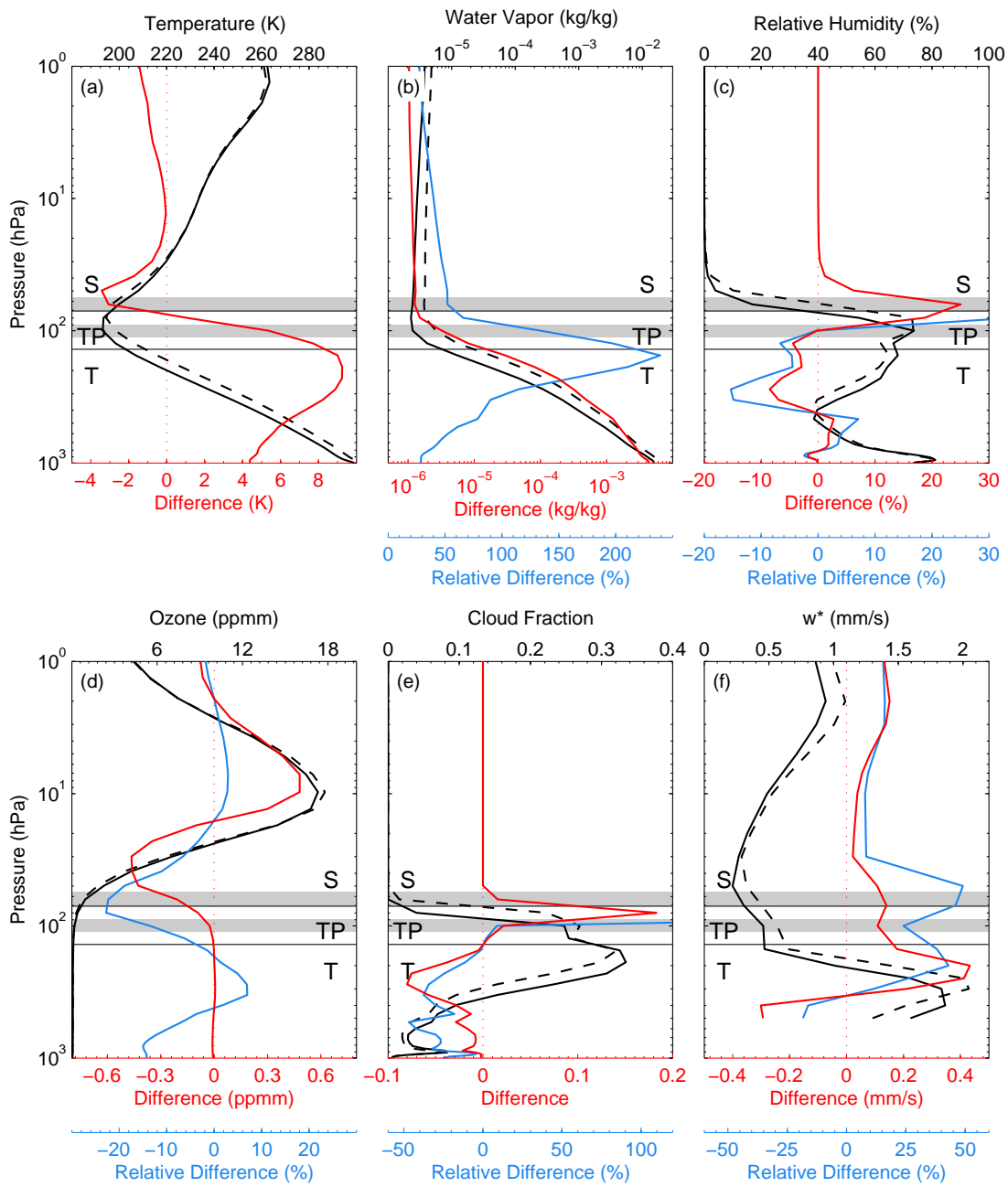


FIG. 5. As in Fig. 2, except for 4KSST.

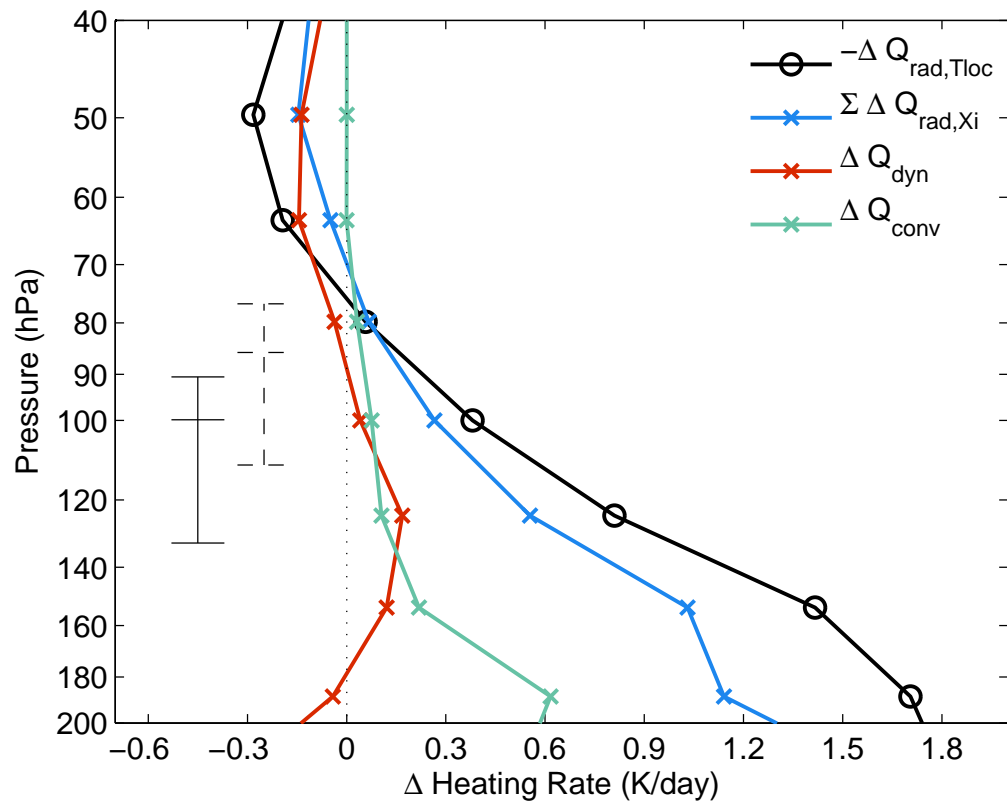


FIG. 6. As in Fig. 3, except for 4KSST.

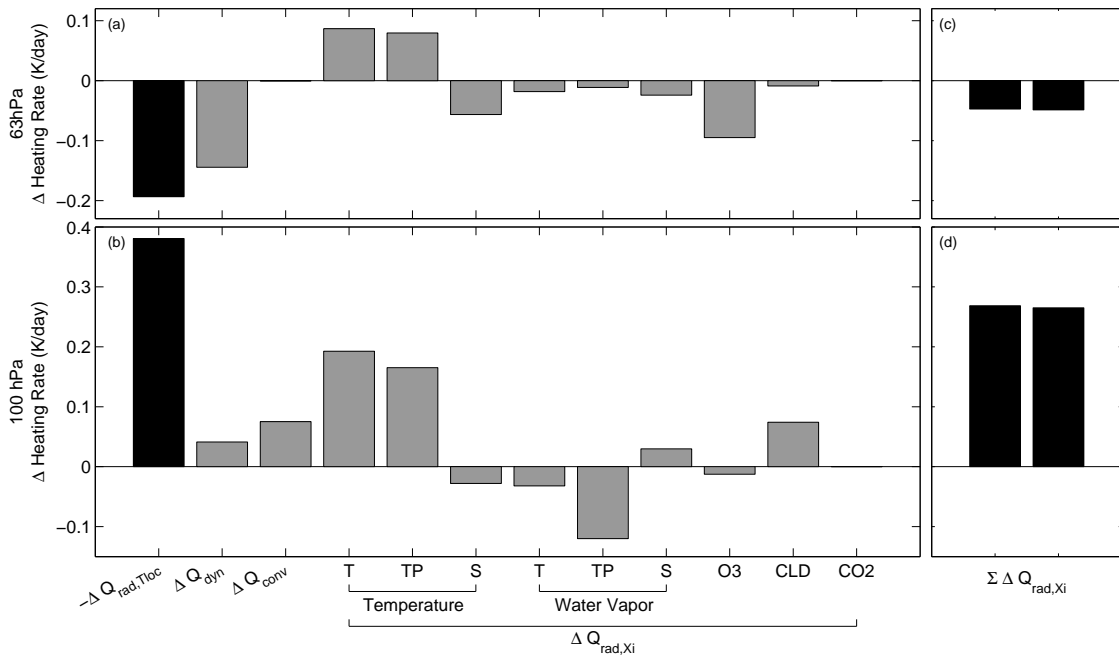
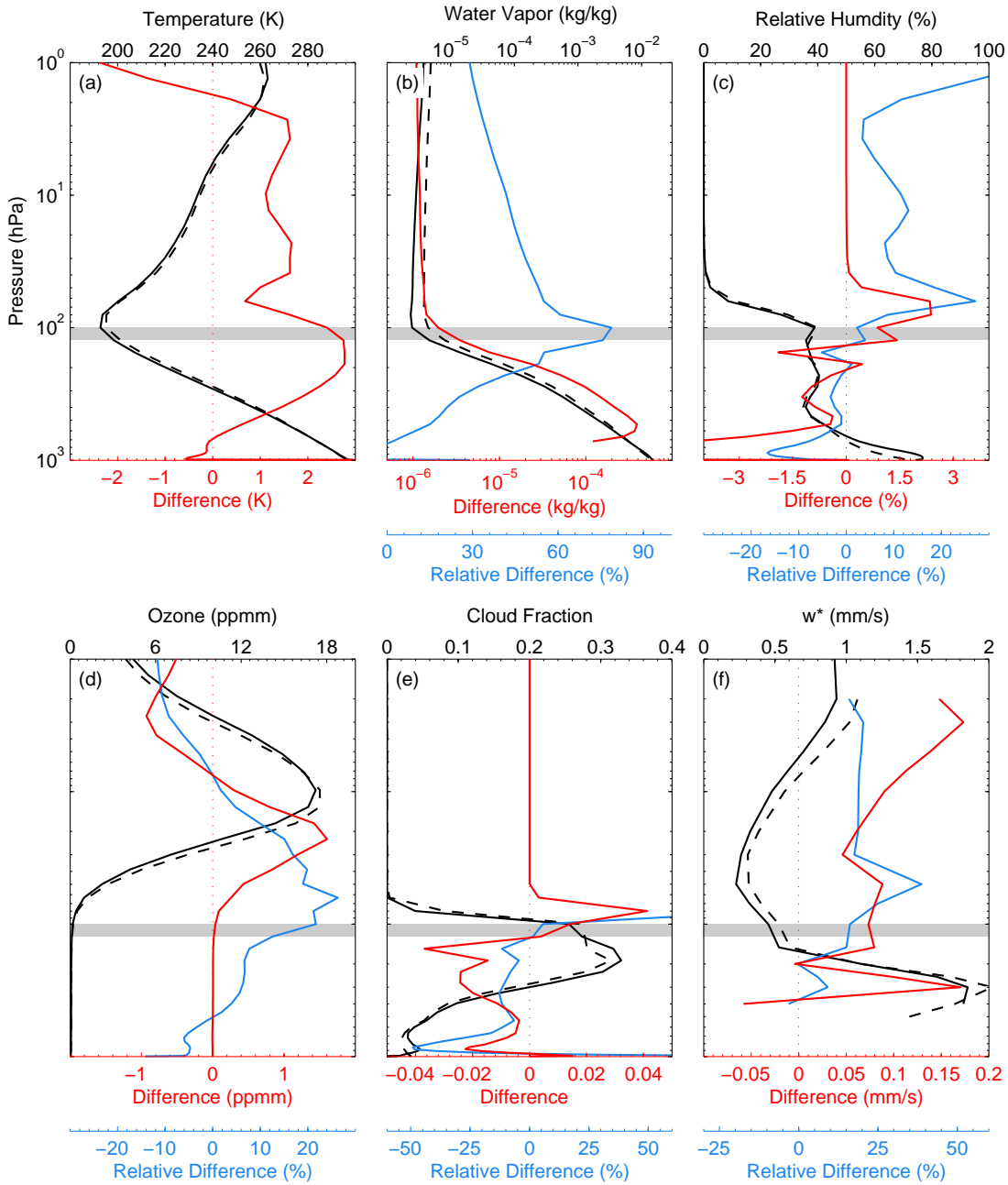


FIG. 7. As in Fig. 4, except for (a) the 63-hPa layer and (b) the 100-hPa layer for 4KSST.



558 FIG. 8. As in Fig. 5, except for in the tropopause-relative coordinate. The gray shading indicates the 100-hPa
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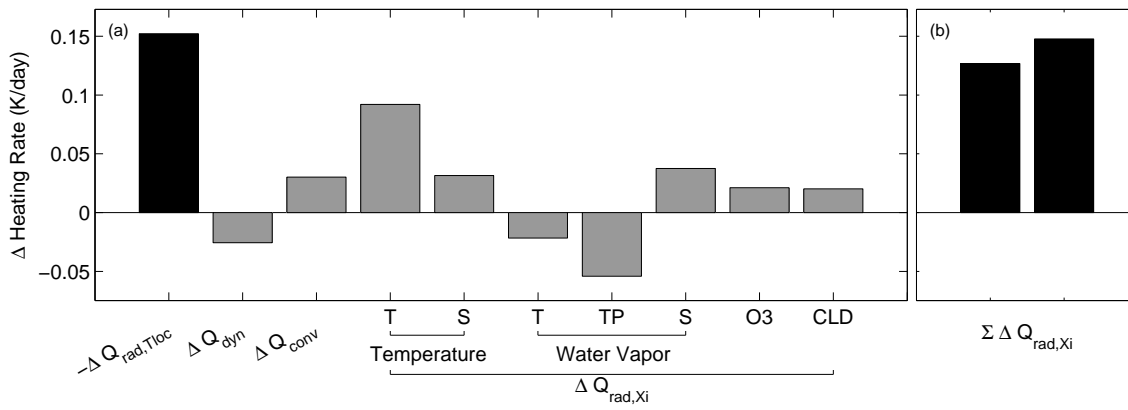
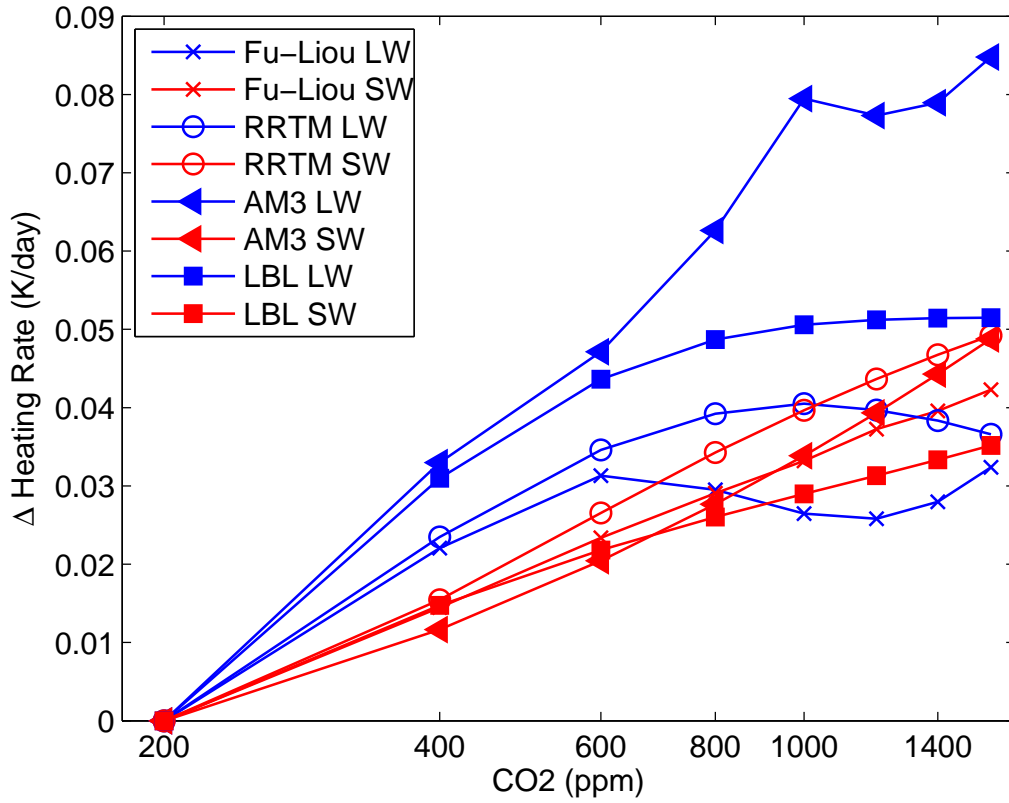


FIG. 9. As in Fig. 7, except for the composite tropopause.



560 FIG. 10. Longwave (blue) and shortwave (red) heating rate changes at the tropopause as carbon dioxide
 561 concentration increases from 200 ppm. The heating rates are calculated using AM3 radiative transfer code
 562 (triangle), Fu-Liou radiative transfer code (cross), the RRTM (circle) and the RFLM line-by-line code (square).
 563 The radiative calculations are done using the tropical mean profiles from the control simulation, and are carried
 564 out at the equinox under clear-sky aerosol-free conditions. See text for more explanation.

Changes of the tropical tropopause layer under global warming: Supplementary Material

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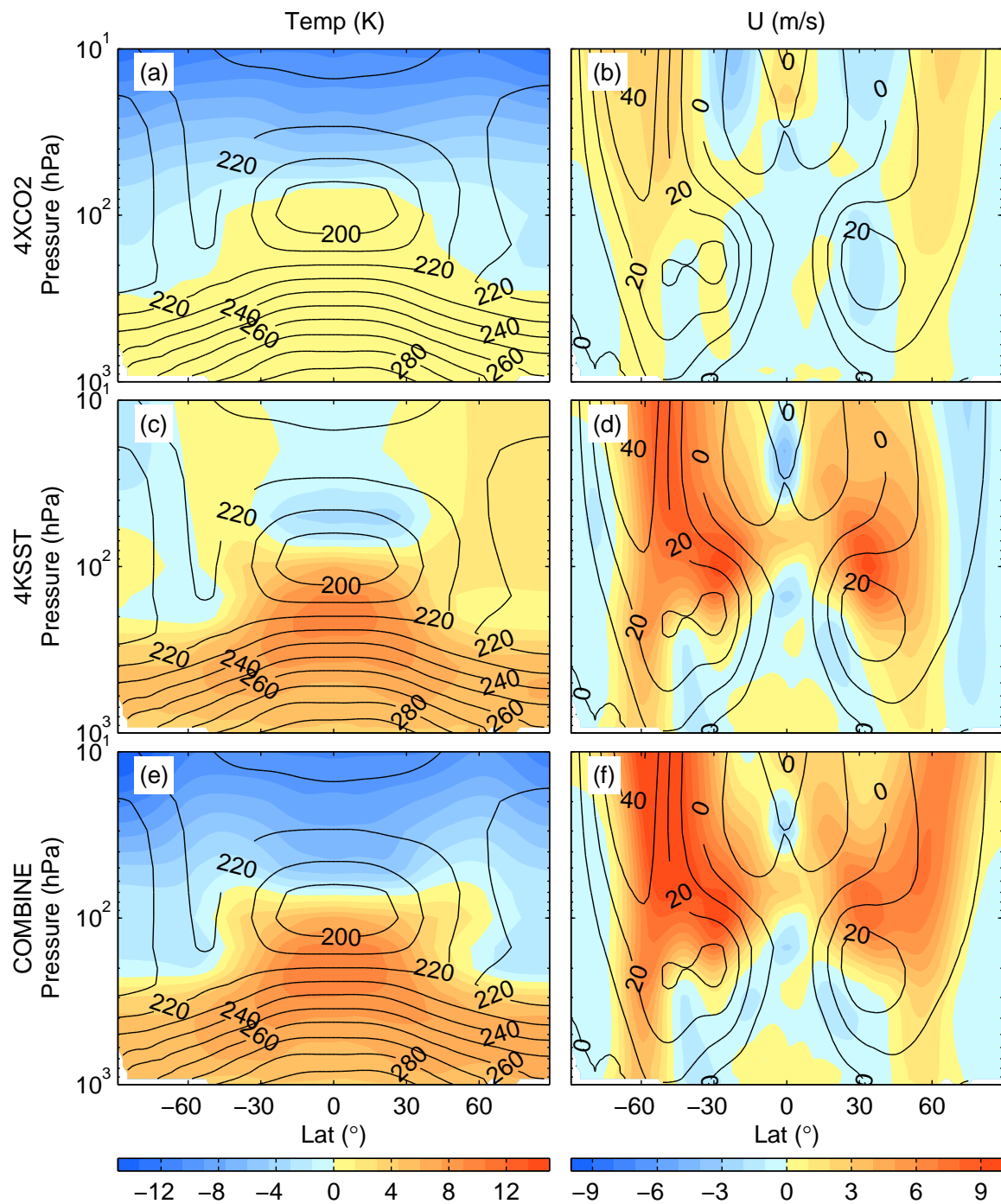


Figure S1. (a) Zonal mean temperature changes from the 4xCO₂ experiment (color shading) and the climatology from the control simulation (black contours). (c) As in (a), except for 4KSST. (e) As in (a), except for COMBINE. (b) (d) and (f), as in (a) (c) and (d), except for zonal wind.