

1 **Modeling Water Vapor and Clouds in an Idealized GCM**

2 YI MING * AND ISAAC M. HELD

Geophysical Fluid Dynamics Laboratory/NOAA, Princeton, NJ

* *Corresponding author address:* Yi Ming, Geophysical Fluid Dynamics Laboratory/NOAA, P. O. Box 308, Princeton, NJ 08542.

E-mail: Yi.Ming@noaa.gov

ABSTRACT

3
4 This paper introduces an idealized general circulation model (GCM) in which water vapor
5 and clouds are tracked as tracers, but are not allowed to affect circulation either through
6 latent heat release or cloud radiative effects. The cloud scheme includes an explicit treatment
7 of cloud microphysics and diagnoses cloud fraction from a prescribed sub-grid distribution
8 of total water. The model is capable of qualitatively capturing many large-scale features of
9 water vapor and cloud distributions outside of the boundary layer and deep tropics. The
10 subtropical dry zones, mid-latitude storm tracks and upper-tropospheric cirrus are simulated
11 reasonably well. The inclusion of cloud microphysics (namely rain re-evaporation) has a
12 significant effect of moistening the lower troposphere in this model. When being subjected
13 to a uniform fractional increase of saturated water vapor pressure, the model produces little
14 change in cloud fraction. A more realistic perturbation, which considers the non-linearity
15 of the Clausius-Clapeyron relation and spatial structure of CO₂-induced warming, results in
16 a substantial reduction in the free-tropospheric cloud fraction. This is reconciled with an
17 increase of relative humidity by analyzing the probability distributions of both quantities.
18 The implications of these results and the utility of the idealized model for understanding
19 cloud feedback are discussed.

20 1. Introduction

21 A complicating factor in simulating and understanding the climatic roles of water vapor
22 (WV) and clouds is their tight coupling with circulation, posing a major bottleneck in nar-
23 rowing the uncertainty of cloud feedback (Bony et al. 2015). This motivates us to construct
24 a model of passive WV and clouds, meaning that both are advected as tracers that do not
25 feed back on circulation either through latent heat release or through cloud radiative effects
26 (CRE). Such a model can be thought of as part of a model hierarchy designed for elucidating
27 the complex interplay between moisture and circulation (Held 2005).

28 Besides cloud feedback, this model may help address what factors have the potential
29 to control the distribution of tropospheric WV. Sun and Lindzen (1993) postulated that
30 tropical relative humidity (RH) was influenced significantly by cloud microphysics, in par-
31 ticular re-evaporation of hydrometeors. This view was later countered by a body of literature
32 collectively known as the advection-condensation theory (Salathé and Hartmann 1997; Pier-
33 rehumbert et al. 2007, and references therein), which put more emphasis on circulation and
34 succeeded in reproducing some gross features of RH. These studies typically used simple
35 saturation adjustment (i.e. WV in excess of saturation being removed instantaneously as
36 surface precipitation), and did not include explicit cloud microphysics. Models with passive
37 WV and clouds would allow us to re-evaluate the relative importance of cloud microphysics
38 and circulation in setting tropospheric RH in a self-consistent framework.

2. Model Description and Experimental Design

The model described here is an example of a class of models that can be constructed based on an atmospheric dry dynamical core coupled with a GCM's cloud physics, or with more simplified or more complex versions of the latter. There is no convective parameterization. The large-scale flow is unaffected by the WV and cloud fields. In theory the flow could be stored offline and read into the model as needed but this is typically inconvenient.

Our example of such a model (referred to as the cloud model here) is forced thermally to a prescribed equilibrium temperature profile via Newtonian relaxation, and, as there is no explicit boundary layer parameterization, wind fields are damped by Rayleigh friction near the surface, precisely as in Held and Suarez (1994). Three water tracers are advected: specific humidity, liquid and ice condensates. Surface evaporation is mimicked by nudging RH below ~ 850 hPa to 100% with a time scale of 30 minutes. The large-scale cloud scheme is the same as implemented in the Geophysical Fluid Dynamics Laboratory (GFDL) HiRAM model (Zhao et al. 2009). Cloud fraction and condensation are diagnosed from grid-mean total water (WV and cloud condensates) using an assumed subgrid-scale distribution, which takes the form of a beta distribution with the width controlled by the grid-mean total water multiplied by a width parameter, just as in Tompkins (2002). The shape parameters p and q in Eq. (7) of Tompkins (2002) are set at 5, resulting in a symmetrical distribution; the width parameter is set at 0.2 in our control simulation. Cloud microphysics is adopted from Rotstayn (1997) and Rotstayn et al. (2000), same as in GFDL AM2 (The GFDL Global Atmospheric Model Development Team 2004) and AM3 models (Donner et al. 2010). This single-moment scheme takes into account the main pathways for transformations between

61 cloud condensates, precipitation formation, and re-evaporation of condensates and precipi-
62 tation. Condensation (re-evaporation) is assumed not to generate latent heating (cooling),
63 and thus does not affect flow. There are no cloud or WV radiative effects as no explicit
64 radiation is involved. In this sense, WV and clouds are completely passive. Using the cloud
65 scheme from a particular full GCM in this way is a test of concept. Examining a whole
66 variety of microphysical schemes may be of interest in this context, varying from much more
67 idealized schemes, to the schemes used in other GCMs, to bin-microphysical models.

68 The model analyzed here has a spectral dynamical core with a horizontal resolution of
69 T42, and 20 equally spaced vertical sigma layers. There is no claim that this simulation
70 is converged as horizontal and especially vertical resolution is increased. Studies of the
71 dependence of results such as these on resolution, and the dynamical core more generally,
72 will hopefully be facilitated by this model configuration. The algorithm for tracer advection
73 is identical to that used for passive tracer advection with this spectral dynamical core in the
74 past (e.g. Galewsky et al. 2005; Polvani and Esler 2007). Since it has not been documented
75 in those studies, we describe it in a short appendix.

76 In an alternative model configuration (referred to as the saturation adjustment model),
77 the cloud scheme is replaced with saturation adjustment. The only water tracer is specific
78 humidity. As any newly formed condensate is assumed to fall out of the air immediately, this
79 model, which is similar to that used in Galewsky et al. (2005), cannot be used to simulate
80 clouds. We perform control simulations with these two models (referred to as CNTL-C and
81 CNTL-SA, respectively). The RH difference between them tells us how the inclusion of
82 the cloud scheme influences the distribution of tropospheric WV. To further separate the
83 influences of cloud macrophysics (partial cloudiness in the cloud model vs. full cloudiness in

84 the saturation adjustment model) and microphysics (present in the cloud model vs. absent
85 from the saturation adjustment model), we design a sensitivity experiment with the cloud
86 model, in which the aforementioned width parameter is lowered to 0.01. This has an effect
87 of allowing for cloud formation only when grid-mean RH essentially reaches 100%, thus
88 switching from zero to full cloudiness (saturation adjustment). This experiment is referred
89 to as NW (Narrower Width). The difference between CNTL-C and NW can be attribute to
90 the change of cloud macrophysics, while the inclusion of cloud microphysics results in the
91 difference between NW and CNTL-SA.

92 In order to explore the responses of WV and clouds to increased saturated water vapor
93 pressure (e_s), we carry out three perturbation experiments with the default cloud model. In
94 the first one (referred to as UN, UNiform), e_s used in moist physics and diagnosis (e.g. RH)
95 (denoted as e_s^*) is increased uniformly by 14%, regardless of temperature T :

$$e_s^*(T) = 1.14e_s(T). \quad (1)$$

96 This is motivated by the commonly held notion that e_s increases with T approximately by
97 7% K⁻¹, a useful starting point for thinking about the hydrological response to CO₂-induced
98 warming. In this sense, the specified e_s increase represents the thermodynamical effect of
99 a 2 K warming. This, however, is strictly valid only for a temperature range typical of
100 the surface. The second experiment (referred to as TS, Temperature Square) relaxes this
101 restriction by taking into account the temperature-dependence of the Clausius-Clapeyron
102 relation:

$$e_s^*(T) = 1.14e_s(T) \left(\frac{293}{T} \right)^2. \quad (2)$$

103 At 233 K (representative of the upper troposphere), the percentage increase is about 80%,

104 much larger than at the surface. In the third experiment (referred to as TC, Temperature
 105 Cubic), we further enhance the temperature-dependence from square to cubic to partially
 106 factor in the effect of upper-tropospheric amplification, a consequence of the moist adiabatic
 107 lapse rate, as well as polar amplification. The resulting expression is

$$e_s^*(T) = 1.14e_s(T) \left(\frac{293}{T} \right)^3. \quad (3)$$

108 This further elevates the percentage increase to about 130% for 233 K. For a surface warming
 109 of 2 K, the upper troposphere can be warmer by 5 K in GCMs, which would increase local
 110 e_s by about 200%. Therefore, the cubic dependence still likely underestimates the relative
 111 change of e_s for the upper troposphere.

112 In using this procedure to mimic some of the effects of warming, one must keep in mind
 113 the several ways in which this cannot capture the effects of warming in comprehensive models.
 114 These include the effects of changes in circulation and also the effects of warming on the
 115 ice/liquid partitioning in clouds.

116 3. Results

117 a. Control Simulations

118 A measure of the overall hydrological cycle strength, the global-mean precipitation (evap-
 119 oration) is virtually the same (~ 2.4 mm day $^{-1}$) in CNTL-C and CNTL-SA. Except for small
 120 differences in the deep tropics and mid- to high latitudes, the zonal distributions of precip-
 121 itation and evaporation are also similar (Fig. 1). The precipitation features three distinct
 122 peaks in the deep tropics and over the mid-latitude storm tracks, and is outweighed by evap-

123 oration by a factor of 4 - 5 in the subtropical dry zones. These results confirm that detailed
124 cloud microphysical treatment is not necessary for simulating the large-scale features of the
125 hydrological cycle in these passive models. This does not necessarily imply that the pre-
126 cipitation distribution is unaffected by cloud microphysical assumptions in comprehensive
127 GCMs due to at least two complicating factors. First, the general circulation in the passive
128 models does not vary with cloud microphysics by design. Second, the hydrological cycle in
129 comprehensive GCMs is constrained by the atmospheric radiative balance, while there exists
130 no such constraint in these passive models. In these models, the strength of the hydrological
131 cycle is controlled by the rate of export of WV out of the saturated boundary layer by the
132 circulation. This is true in more comprehensive models as well, but there is no feedback here
133 between the radiative cooling of the free troposphere with the circulation exporting WV out
134 of the boundary layer.

135 A comparison with the aqua-planet simulations performed with the comprehensive GCMs
136 in the Aquaplanet Intercomparison Project [Fig. 3 of Blackburn et al. (2013)] suggests that
137 the cloud model captures many gross features of the global RH distribution, including the
138 subtropical dry zones, dry upper troposphere and moist mid- and high latitudes. The RH in
139 the deep tropics (15°S - 15°N) is too high (over 80%) due to the absence of moist convection
140 either parameterized or resolved, which is the main mechanism of tropical dehydration in
141 comprehensive GCMs. For the same reason, the outflow from the tropical ascent is more
142 spread vertically in this model than in the aqua-planet simulations, causing the subtropical
143 dry zones to be placed lower. Similar conclusions can be drawn by comparing with the
144 comprehensive CMIP3 (Coupled Model Intercomparison Project Phase 3) model results [Fig.
145 1 of Sherwood et al. (2010)]. Replacing saturation adjustment with the cloud scheme tends

146 to moisten the subtropics and mid-latitudes ($15^\circ - 60^\circ$) by a few percent (in absolute RH)
147 (the lower panel of Fig. 2). The drying of the polar upper troposphere can be attributed
148 partly to the treatment of partial cloudiness in the cloud model as described below.

149 The total non-evaporation WV tendency is given in Fig. 3. The three local maxima (the
150 deep tropics and mid-latitudes) correspond to the Intertropical Convergence Zone (ITCZ)
151 and storm tracks (the upper panel). Both models generate similar spatial patterns, substan-
152 tiating that saturation adjustment, as simple as it is, is indeed sufficient for capturing the
153 gross features of precipitation. The biggest differences lie approximately over $\sim 30^\circ - 60^\circ$ and
154 between ~ 500 and 800 hPa; the WV sink (or the condensate source) is stronger in CNTL-C
155 than in CNTL-SA, coinciding with higher surface precipitation associated with storm tracks
156 in the former.

157 A decomposition of the tendency in CNTL-C on the microphysical process level confirms
158 that condensation is the dominant sink of WV, and is responsible for the vast majority of
159 precipitation formation (Fig. 4). Ice deposition takes over in the upper troposphere, but is
160 about one order of magnitude smaller than condensation. Rain re-evaporation, which occurs
161 when falling raindrops enter unsaturated air, is a non-negligible source of WV in the sub-
162 tropical and mid-latitude lower troposphere. A sensitivity experiment with re-evaporation
163 switched off indicates that it is indeed partly responsible for the moistening. (In comparison,
164 cloud liquid re-evaporation is almost negligible, and is not shown.) As another source of WV
165 over the mid-latitudes, snow sublimation is of comparable magnitude, but generally deeper
166 into the atmosphere's interior than re-evaporation.

167 As described in the previous section, NW is an intermediate case between CNTL-C and
168 CNTL-SA. The upper panel of Fig. 5 shows that the consideration of partial cloudiness

169 tends to decrease simulated RH everywhere by allowing cloud and precipitation to form at
170 a lower RH threshold value. The largest reduction (more than 3%) occurs over the high-
171 latitudes, indicating that the different treatment of subgrid variability is responsible for a
172 similar feature of the RH difference between the two control simulations (the lower panel
173 of Fig. 2). The effect of incorporating cloud microphysics can be isolated by comparing
174 NW with CNTL-SA (the low panel of Fig. 5). It has marked spatial structure, with strong
175 moistening in the lower troposphere (especially over $\sim 15 - 60^\circ$), which is also present in
176 the RH difference between CNTL-C and CNTL-SA. This confirms the significant role of
177 microphysics in modifying lower-tropospheric RH in this model.

178 Fig. 6 depicts the simulated cloud fields in CNTL-C. The simulated boundary layer
179 clouds are unrealistic due to the lack of a boundary layer scheme, and we view this model's
180 relevance as restricted to the free troposphere. The cloud model is capable of qualitatively
181 reproducing some familiar aspects of the highly inhomogeneous global cloud distribution. In
182 the free troposphere, clouds are most prevalent in the mid- and high latitudes (especially
183 over the storm tracks), where the cloud fraction often exceeds 20% and extends vertically
184 through almost the entire tropospheric column. The tropical upper troposphere ($\sim 100 - 300$
185 hPa) is another place with large cloud fraction. As a reminder, the model used here does
186 not have parameterized or resolved convection. In the subtropical dry zones cloud fraction
187 is generally less than 10%. The transition from cloud liquid to ice follows the freezing line.

189 We use the cloud model to explore how RH and clouds would vary with increased e_s .
190 The results are given in Fig. 7. A uniform increase of 14% barely causes any change in RH
191 (UN minus CNTL-C, the upper panel); WV increases approximately by the same percentage
192 as e_s . The inherent non-linearity of the Clausius-Clapeyron relation (i.e. the temperature
193 dependence of the fractional increase of e_s per degree of warming) gives rise to appreciable
194 increase of free tropospheric RH, which amounts to more than 1% in the subtropical dry zones
195 and mid-latitude lower troposphere (TS minus CNTL-C, the middle panel). An attempt to
196 take into account the additional effect of upper tropospheric and polar warming (TC minus
197 CNTL-C, the lower panel) amplifies the same pattern seen in TS.

198 The corresponding changes in cloud fraction are shown in Fig. 8. There is almost no
199 change in UN (the upper panel), consistent with the muted response in RH. Both TS and
200 TC give rise to marked reductions of similar spatial pattern. In the latter experiment, cloud
201 fraction decreases by up to 2% in the subtropical dry zones. The entire free troposphere over
202 $\sim 30^\circ - 50^\circ$ also undergoes substantial reduction of cloud fraction ($\sim 2\%$). This trend extends
203 to the high-latitude upper troposphere. The result that cloud fraction decreases despite
204 higher RH is counter-intuitive; they decrease together in comprehensive GCM comparisons
205 (Zelinka et al. 2013). From the perspective of cloud parameterization, the idealized model
206 effectively diagnoses cloud fraction from RH since WV is usually much larger than the cloud
207 condensates.

208 To better understand the opposing RH and cloud fraction changes, we examine the prob-
209 ability distributions of instantaneous RH and cloud fraction for a domain between 15° and

210 45°N and between 600 and 700 hPa (Fig. 9). The RH distribution (the upper panel) is remi-
 211 niscent of that produced with the back trajectory technique [Fig. 6.17 of Pierrehumbert et al.
 212 (2007)]. Unlike the specific GCM used in Pierrehumbert et al. (2007), the idealized model,
 213 despite being low-resolution, simulates a strong dry spike in the probability distribution of
 214 RH. As RH increases, its occurrence becomes less frequent. Only occasionally does RH rise
 215 above 80%, the approximate threshold for cloud formation in the default cloud model. The
 216 vast majority of the samples are cloud-free (the lower panel). The cloud fraction distribution
 217 is relatively flat all the way to $\sim 80\%$, but with a distinct bump between 80% and 100%.

218 In comparison with CNTL-C, the uneven increase of e_s in TC shifts the dry spike in
 219 RH toward higher RH, accompanied by a marked increase in probability of intermediate
 220 RH (20% to 80%) . At the same time, values higher than 80% become less likely. On
 221 balance, the former outweighs the latter, resulting in an increase of the average RH. The
 222 lower occurrence of RH greater than 80% explains the reduction in the average cloud fraction.
 223 One can rationalize the RH changes using the concept of last saturation (Pierrehumbert et al.
 224 2007). The WV specific humidity (q) of a descending parcel (with its present temperature
 225 denoted as T_1) is the same as the saturated specific humidity (q_s) when it last experienced
 226 saturation (with its temperature denoted as T_0). Thus, its RH at pressure P_1 can be written
 227 as $[e_s(T_0)/e_s(T_1)](P_1/P_0)$, where P_0 is the atmospheric pressure of the parcel when it reaches
 228 the last saturation. If one imposes the increase of e_s in the form of Eq. 3, the perturbed
 229 RH would be $[e_s(T_0)/e_s(T_1)](P_1/P_0)(T_1/T_0)^3$, which is an increase since T_1 is greater than
 230 T_0 for a descending parcel. For an ascending parcel, T_0 is greater than T_1 , meaning that
 231 RH would become smaller with increased e_s if q is conserved. The assumption of constant
 232 q does not hold for precipitating parcels once they are saturated, but the fact that T_0

233 is greater than T_1 for ascending parcels suggests that larger displacements are needed to
234 achieve saturation, resulting in a decrease in RH on average in these ascending parts of the
235 circulation. Parcels drier (wetter) than $\sim 80\%$ RH are typically associated with descending
236 (ascending) motion, the above analysis help explain why the dry parcels become more humid
237 in the two perturbation experiments with spatial variations, while the opposite occurs to the
238 wet ones. The latter is the underlying cause of reduced cloud fraction. These simulations
239 are missing the effects of the increase in depth of the troposphere with warming that reduces
240 the increase in the temperature of last saturation and therefore damps the increase in RH
241 that would otherwise occur.

242 Cloud liquid and ice respond largely in opposite directions (Figs. 10 and 11, respectively).
243 Despite higher RH in the lower free troposphere, cloud liquid generally decreases with cloud
244 fraction. In contrast, cloud ice increases at higher altitudes, more consistent with RH change.
245 Note that the temperature used for partitioning condensate into liquid and ice does not
246 change, the upward shift of the freezing line, which is often discussed in the literature, is
247 not an issue here. Thus, it is not straightforward to compare these results with full GCM
248 simulations.

249 **4. Discussion and Conclusions**

250 One can think of the idealized model introduced in this paper as a natural extension
251 of the advection-condensation theory/model that was instrumental for understanding the
252 distribution of tropospheric WV. By decoupling WV and clouds from circulation, the model
253 helps answer to what extent they can be rationalized as being driven by a given circulation.

254 The advection-condensation theory makes the case that circulation is the dominant factor
255 in shaping the large-scale structure of RH. Given the strong link between RH and clouds
256 (cloud fraction in particular), one probably should not be surprised by how well the idealized
257 model is able to reproduce some of the salient features of the global cloud distribution. This
258 suggests that it may be feasible to study the climatology of certain cloud systems (e.g. frontal
259 and cirrus clouds) in a non-interactive mode.

260 A main characteristic of full GCM-simulated response to CO₂-induced warming is a wide-
261 spread reduction of free-tropospheric cloud fraction equatorward of 60° [Fig. 6 of Zelinka
262 et al. (2013)]. This coincides with a reduction of RH [Fig. 2 of Sherwood et al. (2010)],
263 and is usually attributed to circulation changes (namely the poleward shift of storm tracks
264 and the upward expansion of troposphere). It is interesting that the idealized model, when
265 forced cleanly by a purely thermodynamical effect (namely increased saturated water vapor
266 pressure, one of the most robust outcomes of warming), is able to simulate a similar reduction
267 of cloud fraction in the absence of any circulation change. Even more interestingly, the
268 disappearance of clouds is accompanied by an enhancement of average RH. These results are
269 useful for thinking about full GCM-simulated positive cloud feedback. First, although it is
270 reasonable to expect circulation changes to have certain bearings on cloud distribution at the
271 boundaries of circulation regimes, their roles may be somewhat limited within the interiors
272 as warming-induced circulation changes are generally subtle. Second, average RH is not
273 generally a good proxy for cloud fraction as cloud formation is skewed strongly to high RH.
274 Third, the spatial pattern of warming (e.g. upper-tropospheric and polar amplifications)
275 may be effective at altering the probability distribution of both RH and clouds.

276 Much of the literature on cloud feedback is on low boundary layer clouds (e.g. Zhang

277 et al. 2013). Recent studies highlight the roles of parameterized convection in affecting
278 tropospheric cloud condensates and WV through convective detrainment (Sherwood et al.
279 2014; Mauritsen and Stevens 2015; Zhao et al. 2016). Because the idealized model does not
280 have boundary layer or cumulus parameterization, its utility for studying low cloud feedback
281 and possible connection with convection is limited. Equipped with an explicit treatment of
282 cloud microphysics, the model, however, is skillful in simulating the subtropical dry zones.
283 Given how tightly linked free-tropospheric RH and boundary layer clouds are, it could prove
284 to be useful for understanding certain aspects of low cloud feedback.

285 One motivation for suggesting a model with passive WV and clouds in a dry dynamical
286 core is to remove the distinctions in cloud simulations that result from differences in convec-
287 tion schemes in GCMs, allowing a focus on the roles of cloud microphysical and macrophysical
288 (cloud fraction) assumptions. Computations with this class of models may also prove useful
289 in isolating dependencies on the resolution and numerics of the dynamical core arising from
290 the presence of a microphysical package.

291 In conclusion, we present an idealized model that tracks WV and clouds as tracers, but
292 does not allow them to interact with circulation either through latent heat release or CRE.
293 It can simulate many gross features of WV and cloud distributions in extratropical free
294 troposphere. The subtropical dry zones, mid-latitude storm tracks and upper-tropospheric
295 cirrus are captured qualitatively in the simulations. It is found that cloud microphysics
296 (namely rain re-evaporation) plays a modest role in moistening the lower troposphere in this
297 model. An uneven increase of saturated water vapor pressure motivated by global warming
298 simulations has a tendency to reduce free-tropospheric cloud fraction, while RH increases.

299 *Acknowledgments.*

300 The authors thank Peter Phillips for help with model setup, and Michelle Frazer for useful
301 discussion. Ming Zhao and Max Popp kindly reviewed an earlier version of the paper.

302

303

Tracer Advection

304

305 The dynamical core is a standard spectral core with the prognostic variables vortic-
 306 ity, divergence, temperature, and the logarithm of surface pressure with Simmons-Burridge
 307 (Simmons and Burridge 1981) vertical-differencing and with all variables, including the com-
 308 ponents of the velocities, defined at the same grid points (an A-grid) on a latitude-longitude
 309 Gaussian grid. Because the logarithm of surface pressure is the prognostic variable, the
 310 model does not conserve mass exactly.

311 Advecting this model’s passive tracers, WV and especially the condensed water phases
 312 utilized by the microphysics, with spectral advection would contaminate these fields hope-
 313 lessly with Gibb’s ripples. Instead we use a finite-volume grid point advection scheme. We
 314 first write the advection operator in an equivalent “faux flux form” without weighting the
 315 velocity by the pressure thickness (i.e., surface pressure):

$$\mathbf{v} \cdot \nabla \xi = \nabla \cdot (\mathbf{v} \xi) - \xi \nabla \cdot \mathbf{v} \quad (\text{A1})$$

316 The last term is evaluated on the A grid since the spectral model provides the divergence
 317 on this grid. The horizontal faux flux-form transport is computed using the finite volume
 318 formulation of Lin and Rood (LR) (Lin and Rood 1996). The velocities are first linearly
 319 interpolated to the C grid. The horizontal transport is then evaluated assuming a piecewise
 320 linear approximation to the sub-grid distribution of tracer, while the vertical transport uses

321 a piecewise parabolic assumption, with monotonicity limiters as in LR. We also evaluate
322 separately the “integer flux” contribution to the zonal advection, avoiding any time step
323 constraint due to zonal advection, once again as in LR. The latter is necessary for an efficient
324 scheme on the latitude-longitude grid.

325 The spectral model uses leapfrog time step with filtering to avoid separation of even and
326 odd time steps. The tracer advection is adapted to this framework by advecting the tracer
327 over a leapfrog time of $2\delta t$ and using the same Robert filter on the tracer fields.

328 This way of incorporating grid point advection into a spectral model has some awkward
329 features but has advantages in simplicity over other approaches, and shares the problem of
330 non-conservation globally. The quality of this formulation is illustrated by the Polvani and
331 Esler (2007) study of transport of tracers during baroclinic life cycles and the Galewsky et al.
332 (2005) analysis of the sources of subtropical WV, both of which use this algorithm.

333 Our motivation for retaining a spectral core is the exact zonal symmetry of the algorithm,
334 which is an attractive feature for idealized studies such as this in which the model climate
335 should be exactly zonally symmetric in the absence of sampling errors or the (unlikely)
336 non-uniqueness of the climate state. Sensitivity of idealized circulation models carrying
337 a microphysical package to the numerical schemes employed for circulation and for tracer
338 transport, as well as resolution, should be of interest.

REFERENCES

- 341 Blackburn, M., et al., 2013: The aqua-planet experiment (APE): Control SST simulation.
342 *J. Meteorol. Soc. Jpn.*, **91A**, 17–56, doi:10.2151/jmsj.2013-A02.
- 343 Bony, S., et al., 2015: Clouds, circulation and climate sensitivity. *Nature Geosci.*, **8**, 261–268,
344 doi:10.1038/ngeo2398.
- 345 Donner, L. J., et al., 2010: The dynamical core, physical parameterizations, and basic
346 simulation characteristics of the atmospheric component of the GFDL global coupled
347 model CM3. *J. Climate*.
- 348 Galewsky, J., A. Sobel, and I. M. Held, 2005: Diagnosis of subtropical humidity dynamics
349 using tracers of last saturation. *J. Atmos. Sci.*, **62**, 3353–3367.
- 350 Held, I. M., 2005: The gap between simulation and understanding in climate modeling. *B.*
351 *Am. Meteorol. Soc.*, **86**, 1609–1614.
- 352 Held, I. M. and M. J. Suarez, 1994: A proposal for the intercomparison of the dynamical
353 cores of atmospheric general circulation models. *B. Am. Meteorol. Soc.*, **75**, 1825–1830.
- 354 Lin, S.-J. and R. B. Rood, 1996: Multidimensional flux-form semi-lagrangian transport
355 schemes. *Mon. Wea. Rev.*, **124**, 2046–2070.
- 356 Mauritsen, T. and B. Stevens, 2015: Missing iris effect as a possible cause of muted hy-

357 drological change and high climate sensitivity in models. *Nature Geosci.*, **8**, 346–351,
358 doi:10.1038/ngeo2414.

359 Pierrehumbert, R. T., H. Brogniez, and R. Roca, 2007: On the relative humidity of the
360 atmosphere. *The Global Circulation of the Atmosphere*, T. Schneider and A. H. Sobel,
361 Eds., Princeton University Press, 143–185.

362 Polvani, L. M. and J. G. Esler, 2007: Transport and mixing of chemical air masses in idealized
363 baroclinic life cycles. *J. Geophys. Res.*, **112**, doi:10.1029/2007JD008555.

364 Rotstayn, L. D., 1997: A physically based scheme for the treatment of stratiform clouds
365 and precipitation in large-scale models. I: Description and evaluation of microphysical
366 processes. *Quart. J. Roy. Meteor. Soc.*, **123**, 1227–1282.

367 Rotstayn, L. D., B. F. Ryan, and J. Katzfey, 2000: A scheme for calculation of the liquid
368 fraction in mixed-phase clouds in large-scale models. *Mon. Wea. Rev.*, **128**, 1070–1088.

369 Salathé, E. P. and D. L. Hartmann, 1997: A trajectory analysis of tropical upper-tropospheric
370 moisture and convection. *J. Climate*, **10**, 2533–2547.

371 Sherwood, S. C., S. Bony, and J.-L. Dufresne, 2014: Spread in model climate sensitivity
372 traced to atmospheric convective mixing. *Nature*, **505**, 37–42.

373 Sherwood, S. C., W. Ingram, Y. Tsushima, M. Satoh, M. Roberts, P. L. Vidale, and P. A.
374 O’Gorman, 2010: Relative humidity changes in a warmer climate. *J. Geophys. Res.*, **115**,
375 doi:10.1029/2009JD012585.

376 Simmons, A. J. and D. M. Burridge, 1981: An energy and angular-momentum conserving

377 vertical finite-difference scheme and hybrid vertical coordinates. *Mon. Wea. Rev.*, **109**,
378 758–766.

379 Sun, D.-Z. and R. S. Lindzen, 1993: Distribution of tropical tropospheric water vapor. *J.*
380 *Atmos. Sci.*, **50**, 1643–1660.

381 The GFDL Global Atmospheric Model Development Team, 2004: The new GFDL global
382 atmosphere and land model AM2-LM2: Evaluation with prescribed SST simulations. *J.*
383 *Climate*, **17**, 4641–4673.

384 Tompkins, A. M., 2002: A prognostic parameterization for the subgrid-scale variability of
385 water vapor and clouds in large-scale models and its use to diagnose cloud cover. *J. Atmos.*
386 *Sci.*, **59**, 1917–1942.

387 Zelinka, M. D., K. E. T. S. A. Klein, T. Andrews, M. J. Webb, J. M. Gregory, and P. M.
388 Forster, 2013: Contributions of different cloud types to feedbacks and rapid adjustments
389 in cmip5. *J. Climate*, **26**, 5007–5027, doi:10.1175/JCLI-D-12-00555.1.

390 Zhang, M., et al., 2013: CGILS: Results from the first phase of an international project to
391 understand the physical mechanisms of low cloud feedbacks in general circulation models.
392 *J. Adv. Model. Earth Syst.*, **5**, 826–842, doi:10.1002/2013MS000246.

393 Zhao, M., I. M. Held, and G. A. S.-J. Lin and G. A. Vecchi, 2009: Simulations of global
394 hurricane climatology, interannual variability, and response to global warming using a
395 50-km resolution GCM. *J. Climate*, **22**, 6653–6678.

396 Zhao, M., et al., 2016: Uncertainty in model climate sensitivity traced to representations of
397 cumulus precipitation microphysics. *J. Climate*, **29**, 543–560.

398 List of Figures

- 399 1 Zonal-mean precipitation (mm day^{-1} , solid lines) and evaporation (mm day^{-1} ,
400 dotted lines) simulated in CNTL-C (thick lines) and in CNTL-SA (thin lines). 23
- 401 2 RH (%) simulated in CNTL-C (contours in the upper panel) and in CNTL-SA
402 (contours in the lower panel). The difference (defined as the former minus the
403 latter throughout this paper) is shown in color shading in the lower panel. 24
- 404 3 Total water vapor tendency due to phase transition (not including evapora-
405 tion) ($10^{-9} \text{ kg kg}^{-1} \text{ s}^{-1}$) in CNTL-C (contours in the upper panel) and in
406 CNTL-SA (contours in the lower panel). The difference is shown in color
407 shading in the lower panel. White in a colored figure indicates that values are
408 outside the range of the color bar throughout the paper. 25
- 409 4 Water vapor tendencies due to condensation ($10^{-9} \text{ kg kg}^{-1} \text{ s}^{-1}$) (a), ice de-
410 position ($10^{-10} \text{ kg kg}^{-1} \text{ s}^{-1}$) (b), rain re-evaporation ($10^{-10} \text{ kg kg}^{-1} \text{ s}^{-1}$) (c)
411 and snow sublimation ($10^{-10} \text{ kg kg}^{-1} \text{ s}^{-1}$) (d) in CNTL-C. Cloud liquid re-
412 evaporation and ice sublimation are negligible. 26
- 413 5 RH difference (%) between CNTL-C and NW (color shading in the upper
414 panel) and between NW and CNTL-SA (color shading in the bottom panel).
415 The contours represent RH in NW (the upper panel) and in CNTL-SA (the
416 lower panel). 27
- 417 6 Cloud fraction (%), the upper panel), liquid ($10^{-6} \text{ kg kg}^{-1}$, the middle panel)
418 and ice ($10^{-6} \text{ kg kg}^{-1}$, the lower panel) in CNTL-C. 28

- 419 7 RH difference (%) between UN and CNTL-C (the upper panel), between TS
420 and CNTL-C (the middle panel) and between TC and CNTL-C (the lower
421 panel). The contours represent RH in CNTL-C. 29
- 422 8 Cloud fraction difference (%) between UN and CNTL-C (the upper panel),
423 between TS and CNTL-C (the middle panel) and between TC and CNTL-C
424 (the lower panel). The contours represent the cloud fraction in CNTL-C. 30
- 425 9 Normalized histograms of 2-hourly RH (%) and cloud fraction (%) in a domain
426 between 15° and 45°N and between 600 and 700 hPa. The 20 bins are of equal
427 width (5%). The black and red lines represent CNTL-C and TC, respectively.
428 Note that the y-axis of the lower panel is cut off at 0.1. 31
- 429 10 Cloud liquid difference (10^{-6} kg kg⁻¹) between UN and CNTL-C (the upper
430 panel), between TS and CNTL-C (the middle panel) and between TC and
431 CNTL-C (the lower panel). The contours represent the cloud fraction in
432 CNTL-C. 32
- 433 11 Cloud ice difference (10^{-6} kg kg⁻¹) between UN and CNTL-C (the upper
434 panel), between TS and CNTL-C (the middle panel) and between TC and
435 CNTL-C (the lower panel). The contours represent the cloud fraction in
436 CNTL-C. 33

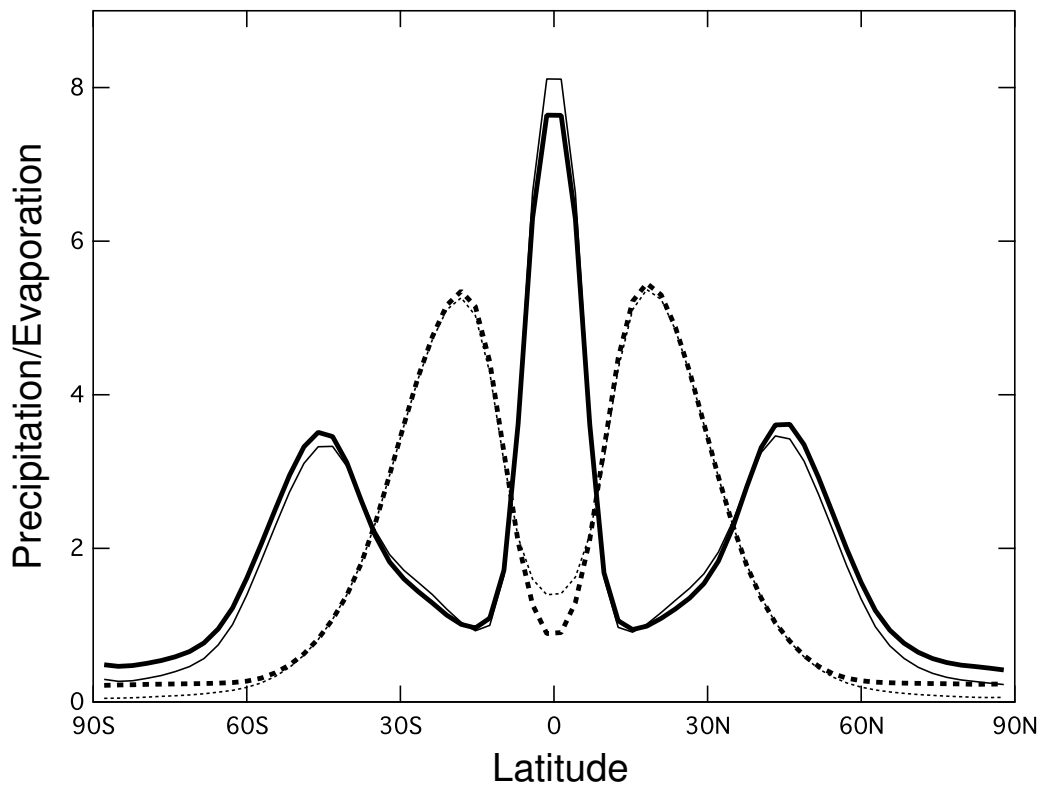


FIG. 1. Zonal-mean precipitation (mm day^{-1} , solid lines) and evaporation (mm day^{-1} , dotted lines) simulated in CNTL-C (thick lines) and in CNTL-SA (thin lines).

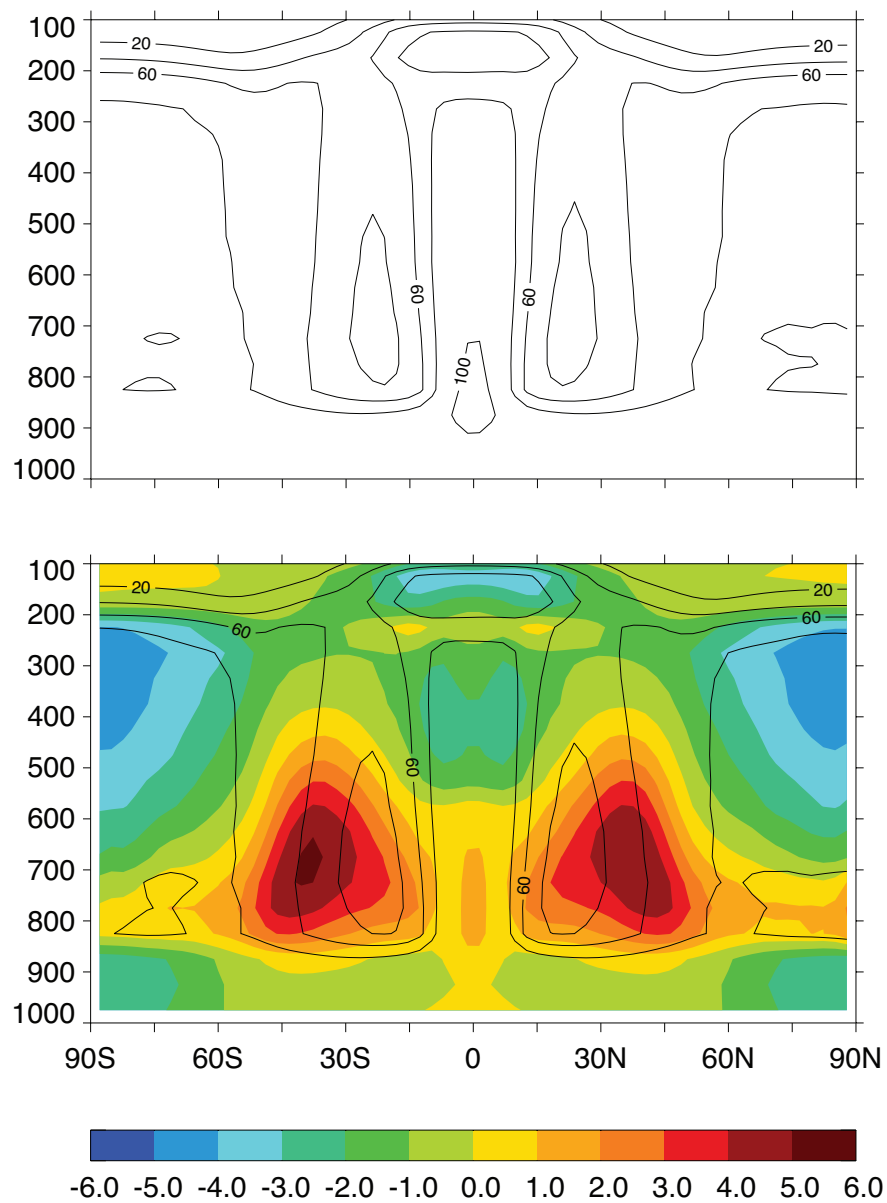


FIG. 2. RH (%) simulated in CNTL-C (contours in the upper panel) and in CNTL-SA (contours in the lower panel). The difference (defined as the former minus the latter throughout this paper) is shown in color shading in the lower panel.

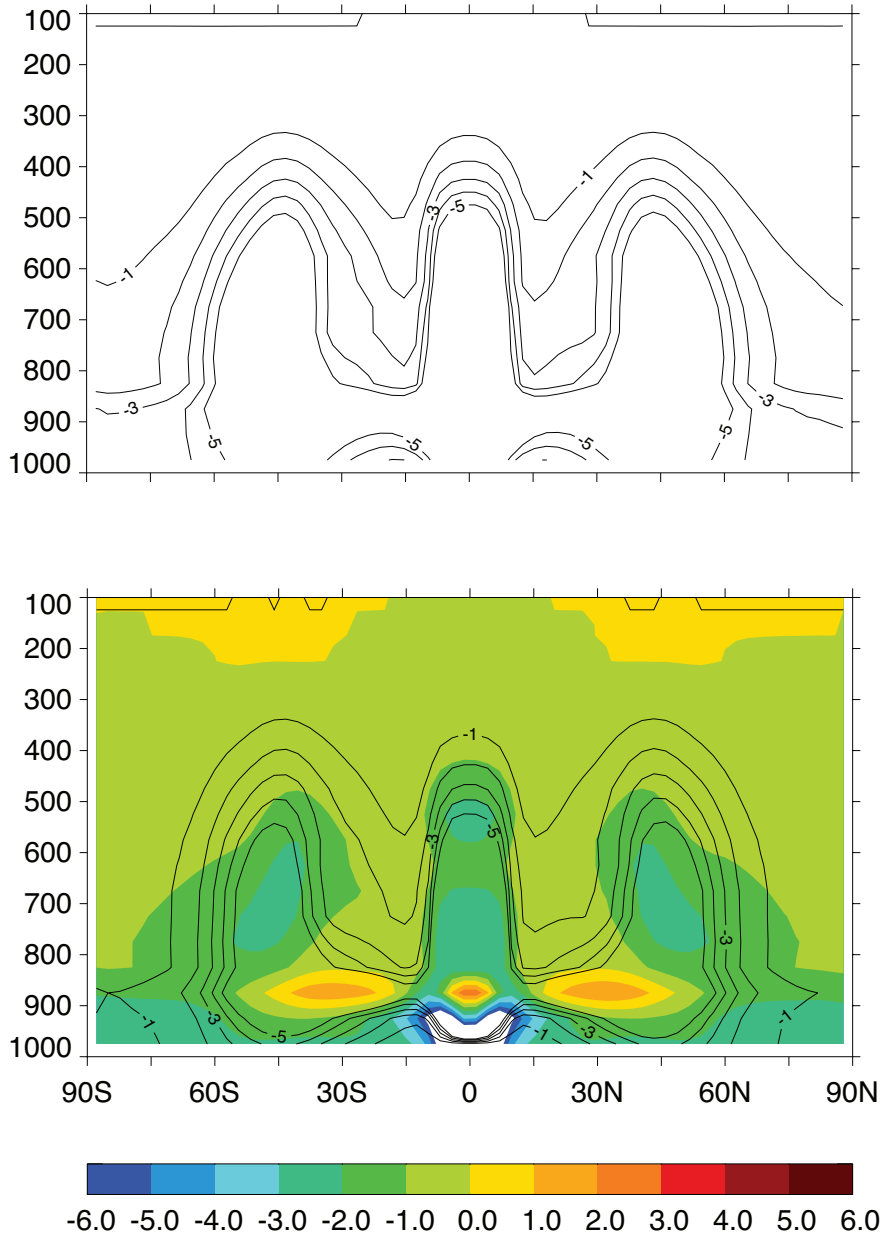


FIG. 3. Total water vapor tendency due to phase transition (not including evaporation) ($10^{-9} \text{ kg kg}^{-1} \text{ s}^{-1}$) in CNTL-C (contours in the upper panel) and in CNTL-SA (contours in the lower panel). The difference is shown in color shading in the lower panel. White in a colored figure indicates that values are outside the range of the color bar throughout the paper.

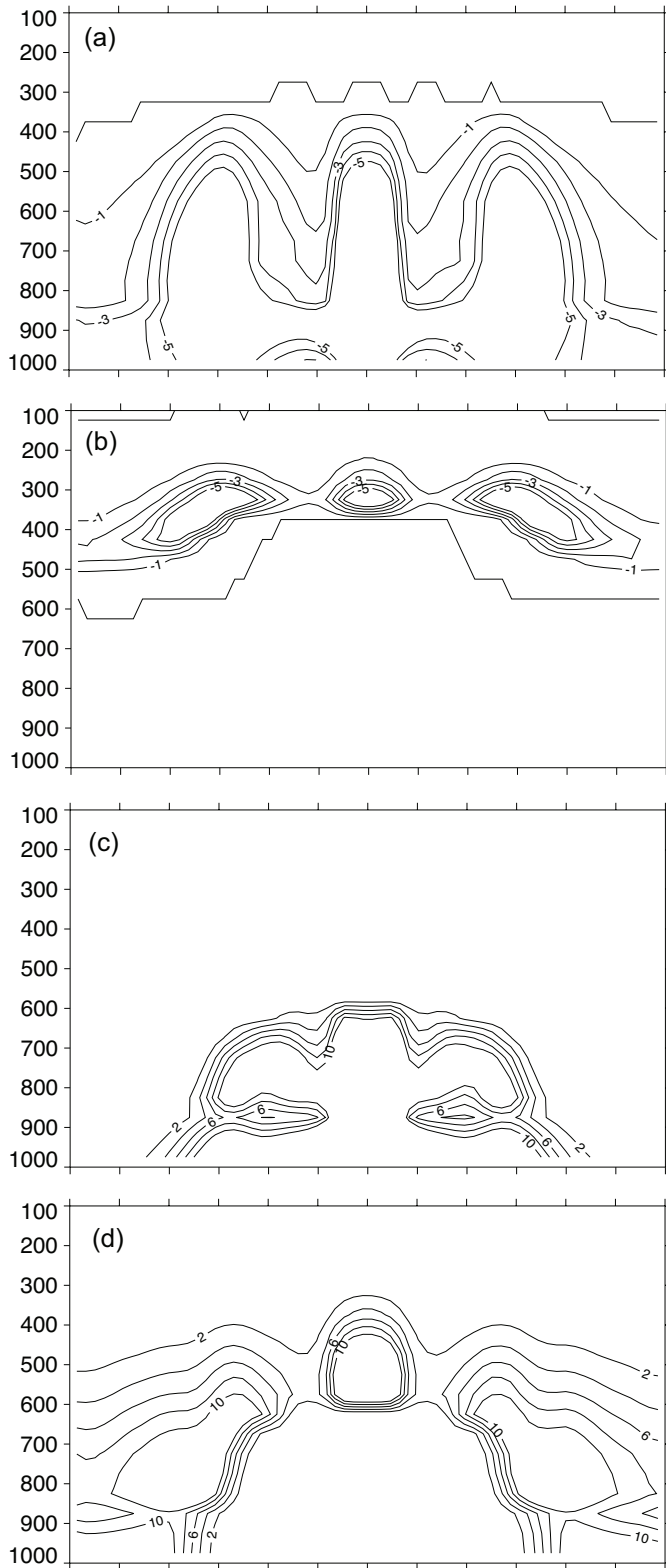


FIG. 4. Water vapor tendencies due to condensation ($10^{-9} \text{ kg kg}^{-1} \text{ s}^{-1}$) (a), ice deposition ($10^{-10} \text{ kg kg}^{-1} \text{ s}^{-1}$) (b), rain re-evaporation ($10^{-10} \text{ kg kg}^{-1} \text{ s}^{-1}$) (c) and snow sublimation ($10^{-10} \text{ kg kg}^{-1} \text{ s}^{-1}$) (d) in CNTL-C. Cloud liquid re-evaporation and ice sublimation are negligible.

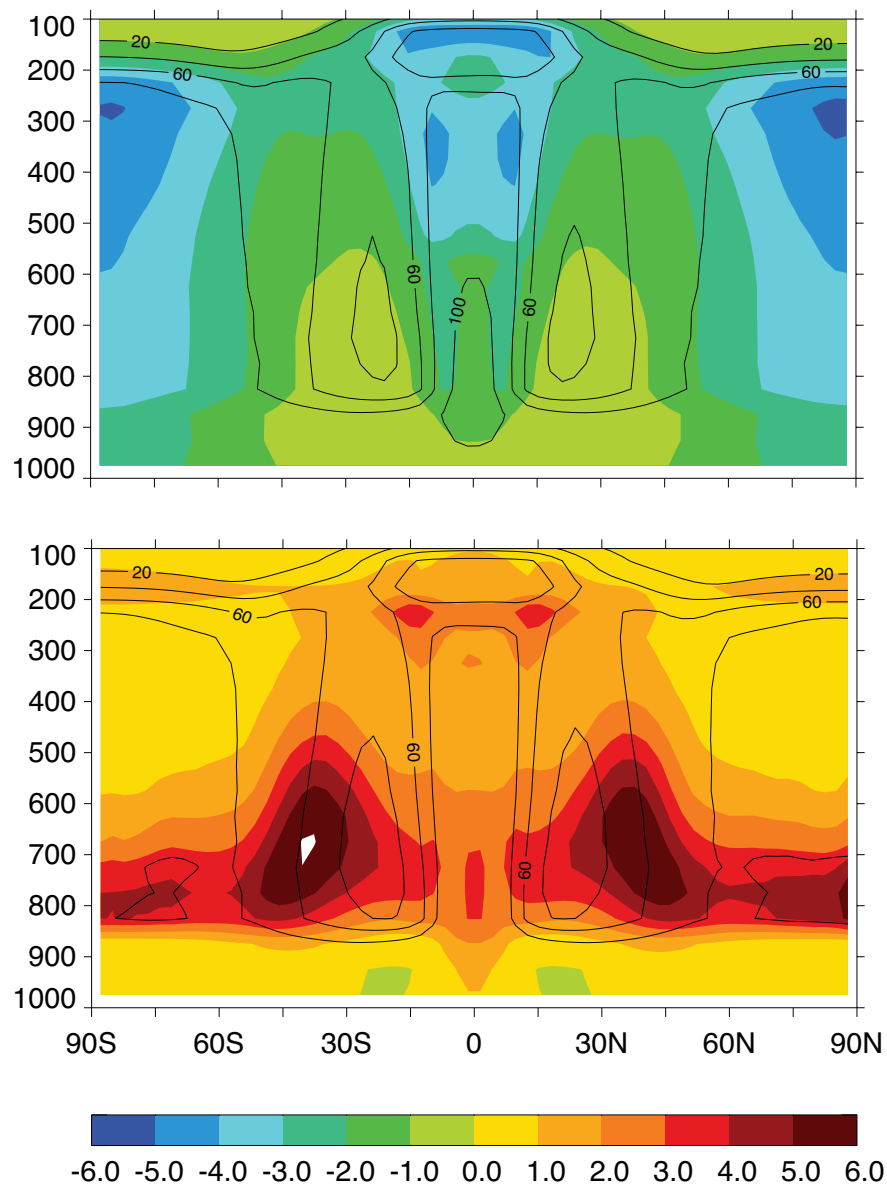


FIG. 5. RH difference (%) between CNTL-C and NW (color shading in the upper panel) and between NW and CNTL-SA (color shading in the bottom panel). The contours represent RH in NW (the upper panel) and in CNTL-SA (the lower panel).

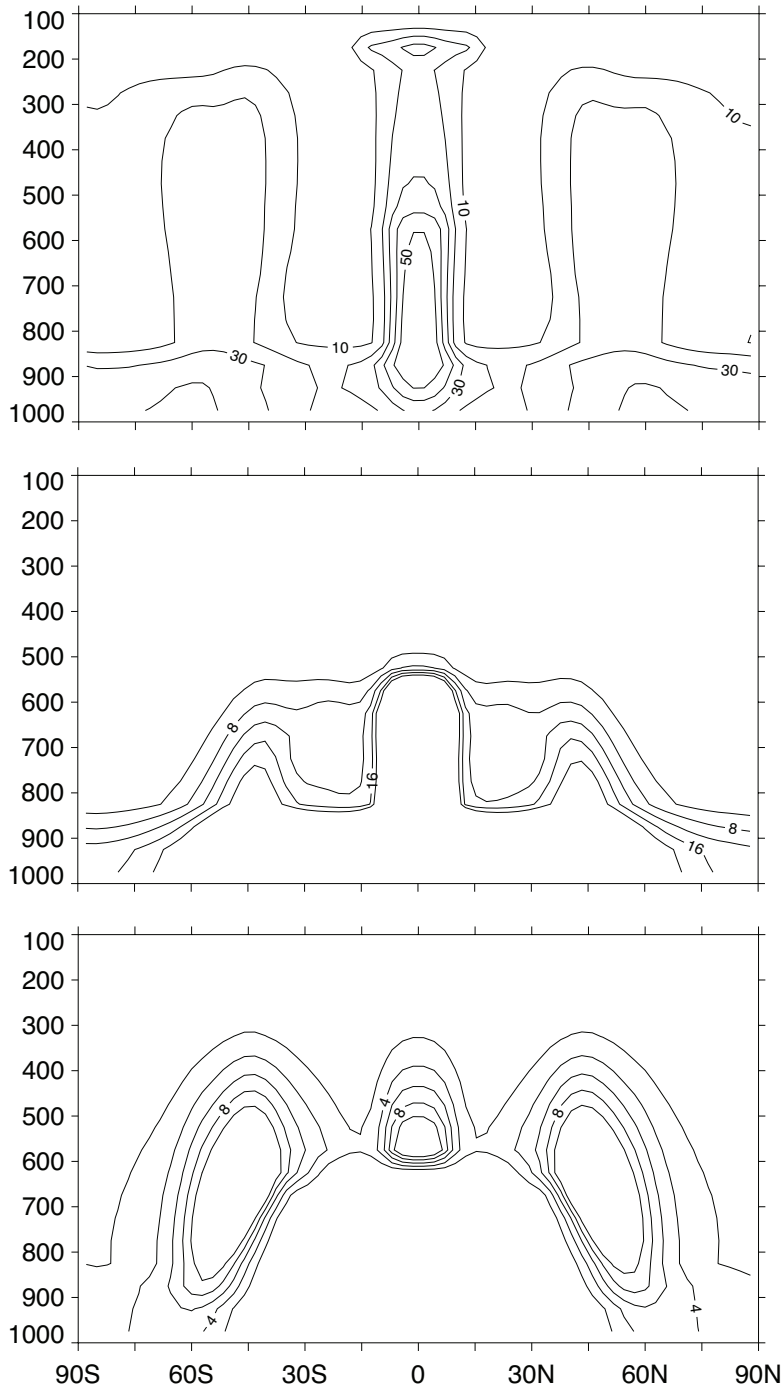


FIG. 6. Cloud fraction (%), the upper panel), liquid ($10^{-6} \text{ kg kg}^{-1}$, the middle panel) and ice ($10^{-6} \text{ kg kg}^{-1}$, the lower panel) in CNTL-C.

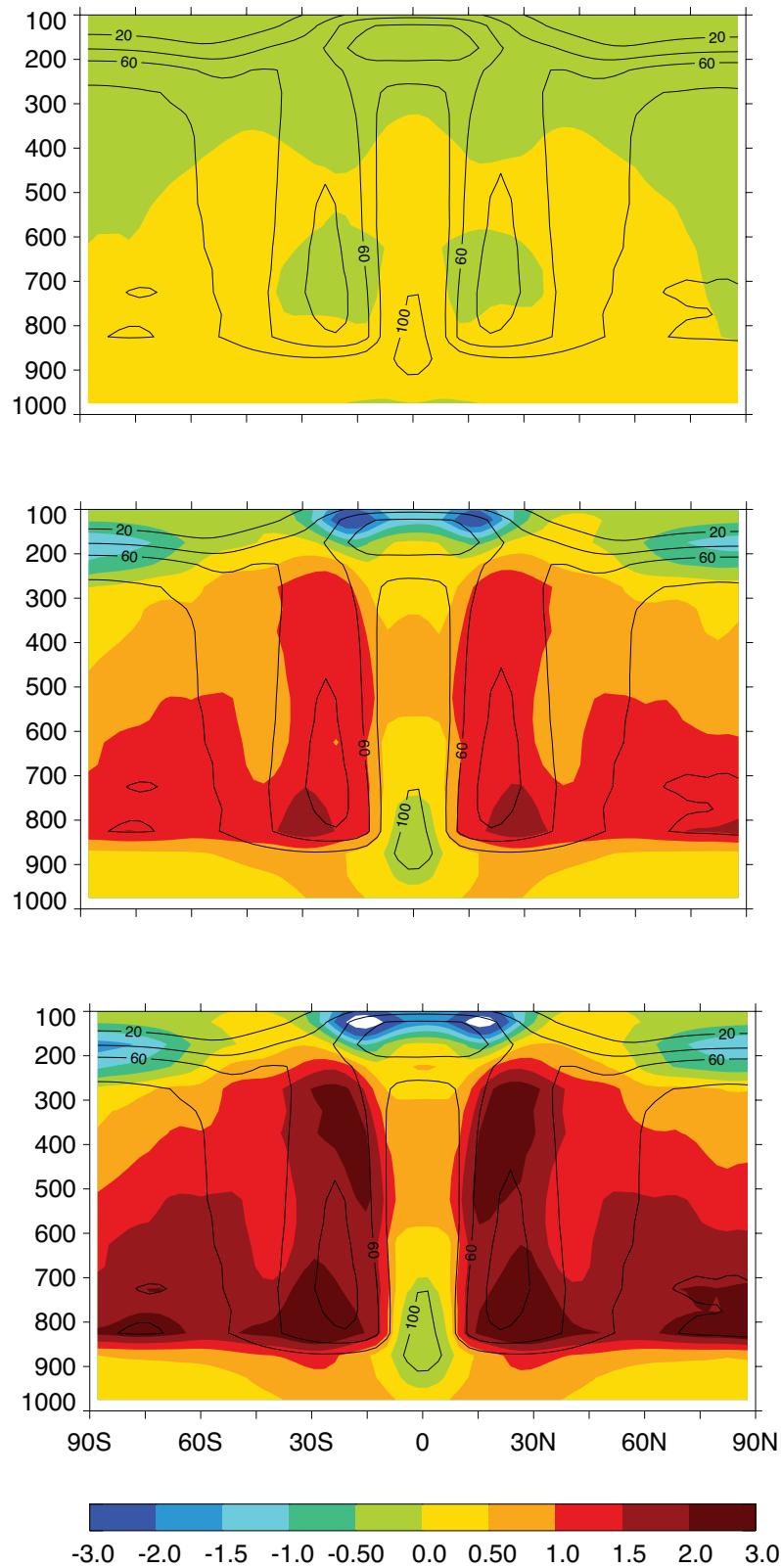


FIG. 7. RH difference (%) between UN and CNTL-C (the upper panel), between TS and CNTL-C (the middle panel) and between TC and CNTL-C (the lower panel). The contours represent RH in CNTL-C.

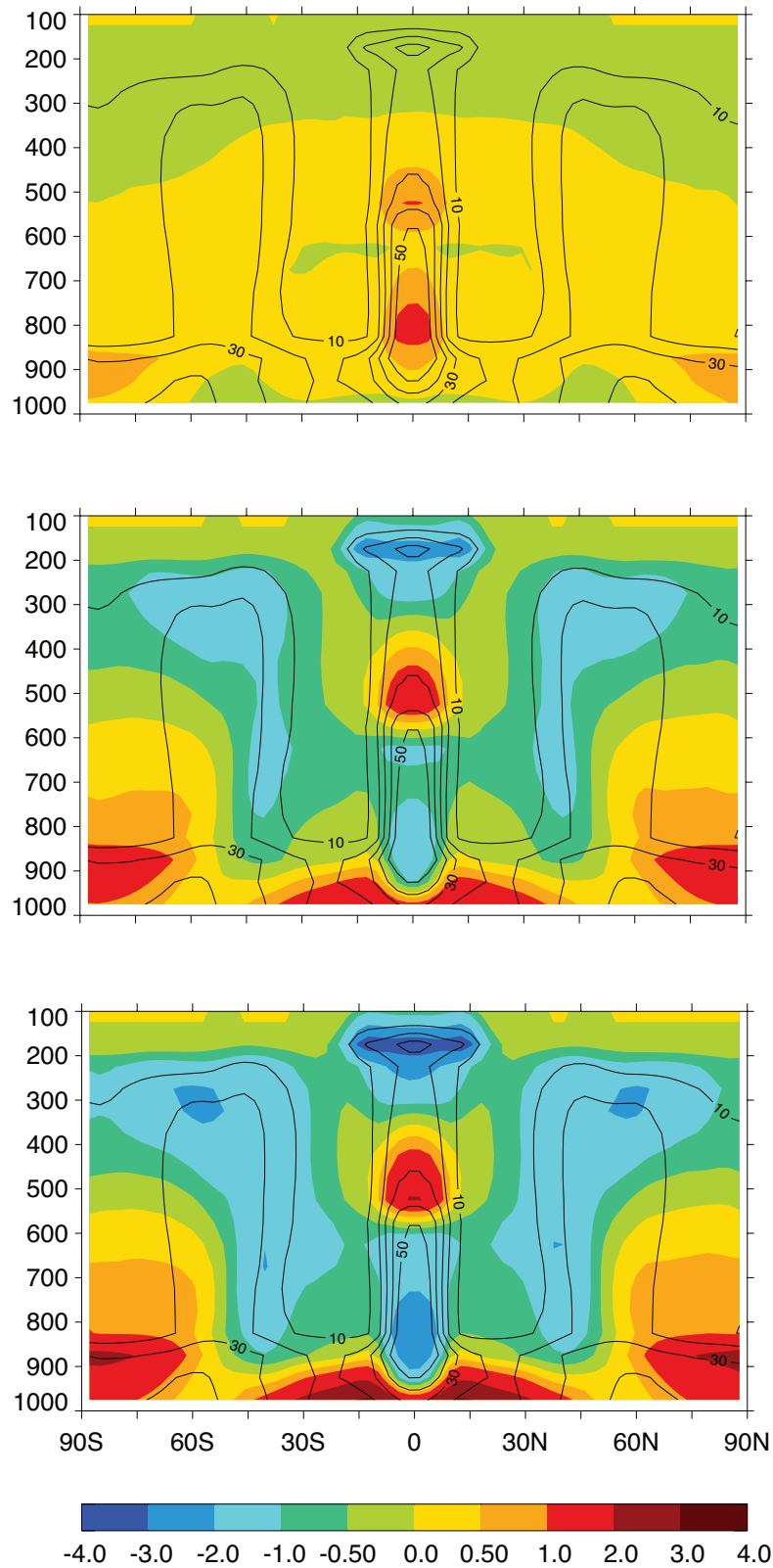


FIG. 8. Cloud fraction difference (%) between UN and CNTL-C (the upper panel), between TS and CNTL-C (the middle panel) and between TC and CNTL-C (the lower panel). The contours represent the cloud fraction in CNTL-C.

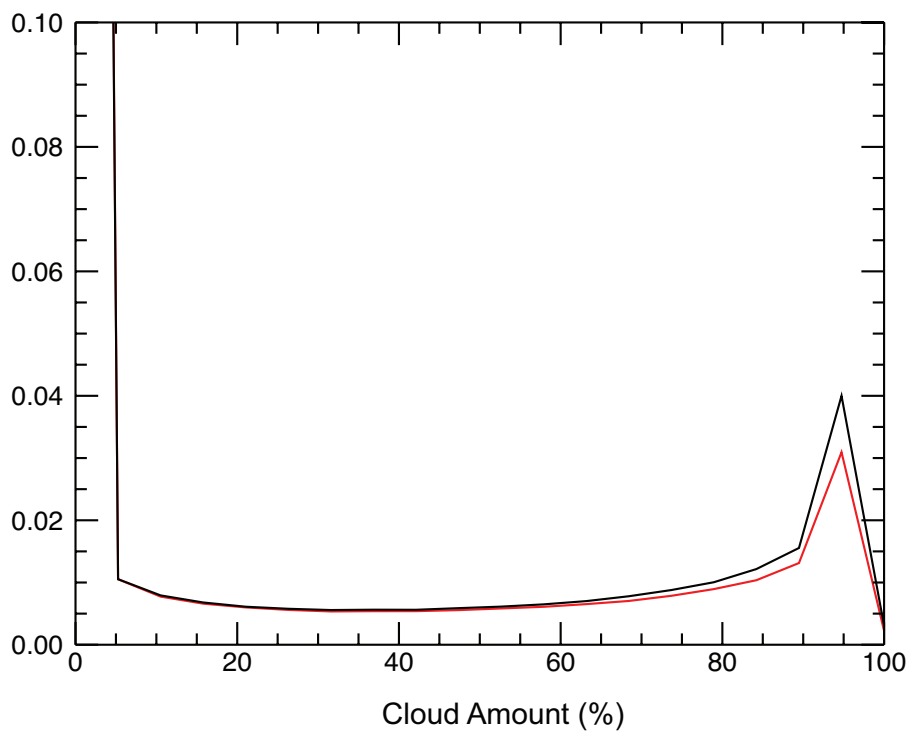
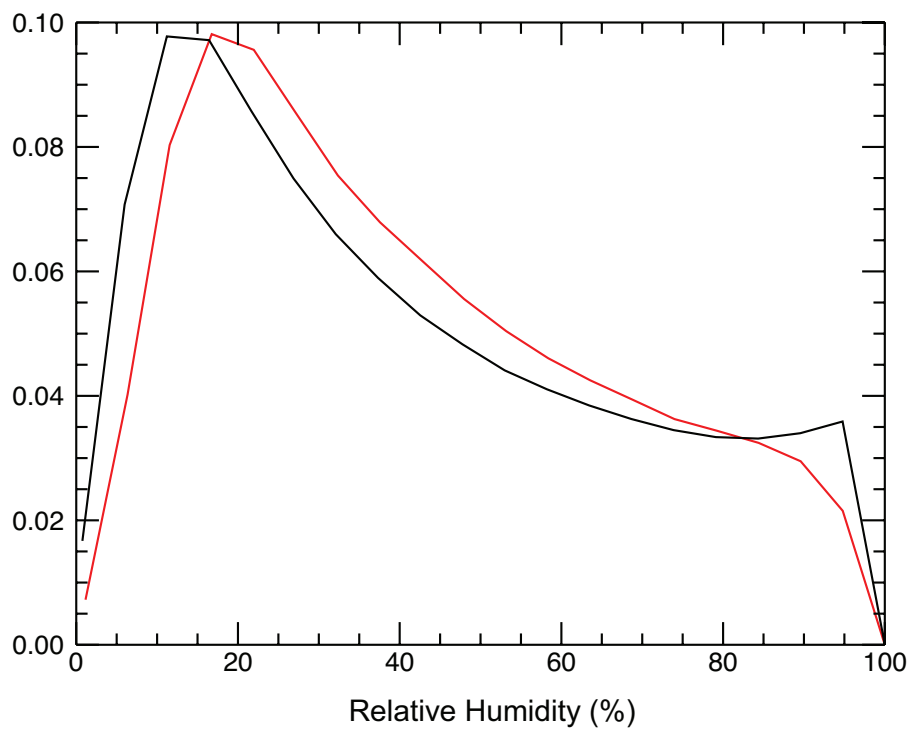


FIG. 9. Normalized histograms of 2-hourly RH (%) and cloud fraction (%) in a domain between 15° and 45° N and between 600 and 700 hPa. The 20 bins are of equal width (5%). The black and red lines represent CNTL-C and TC, respectively. Note that the y-axis of the lower panel is cut off at 0.1.

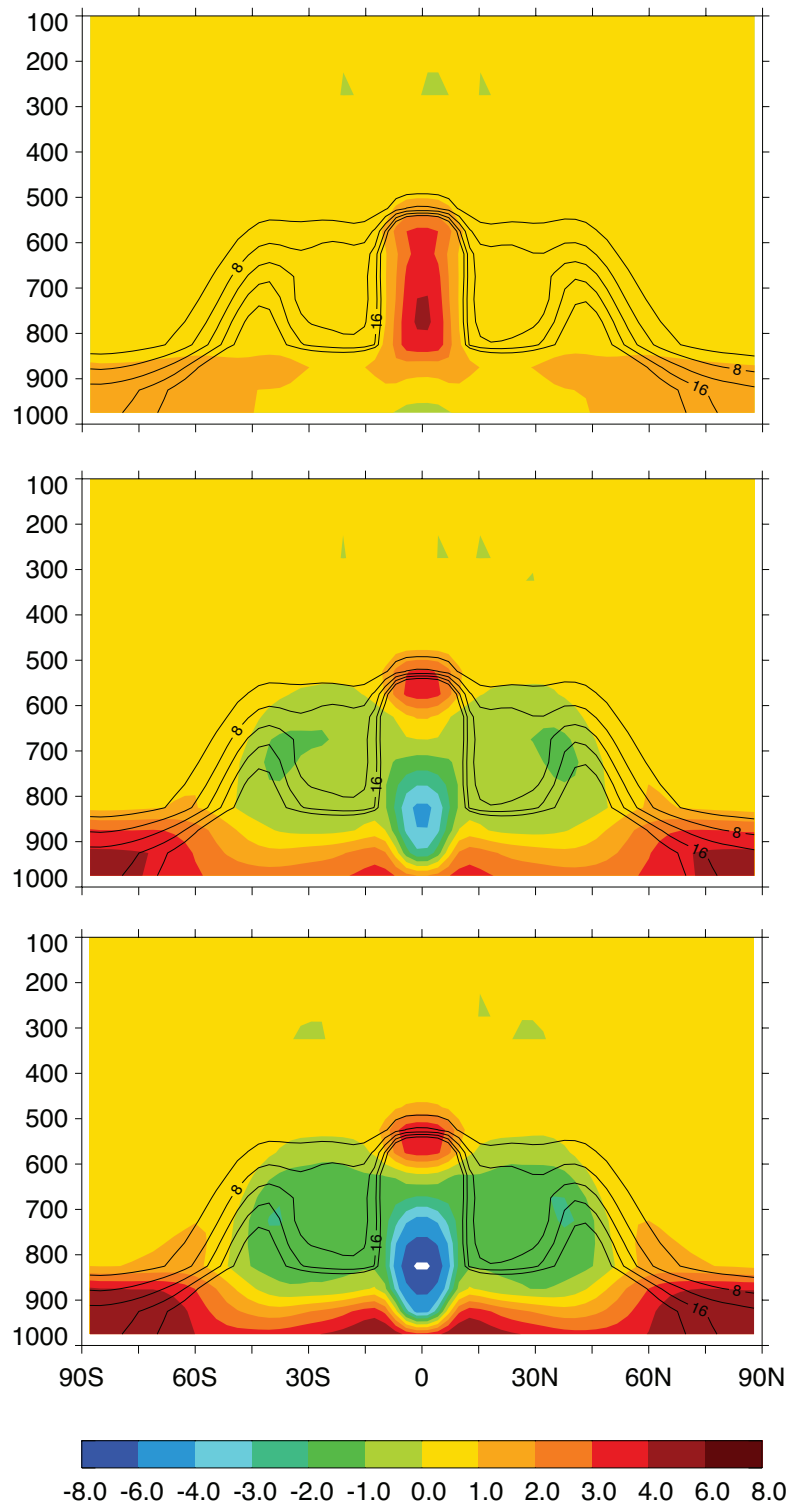


FIG. 10. Cloud liquid difference ($10^{-6} \text{ kg kg}^{-1}$) between UN and CNTL-C (the upper panel), between TS and CNTL-C (the middle panel) and between TC and CNTL-C (the lower panel). The contours represent the cloud fraction in CNTL-C.

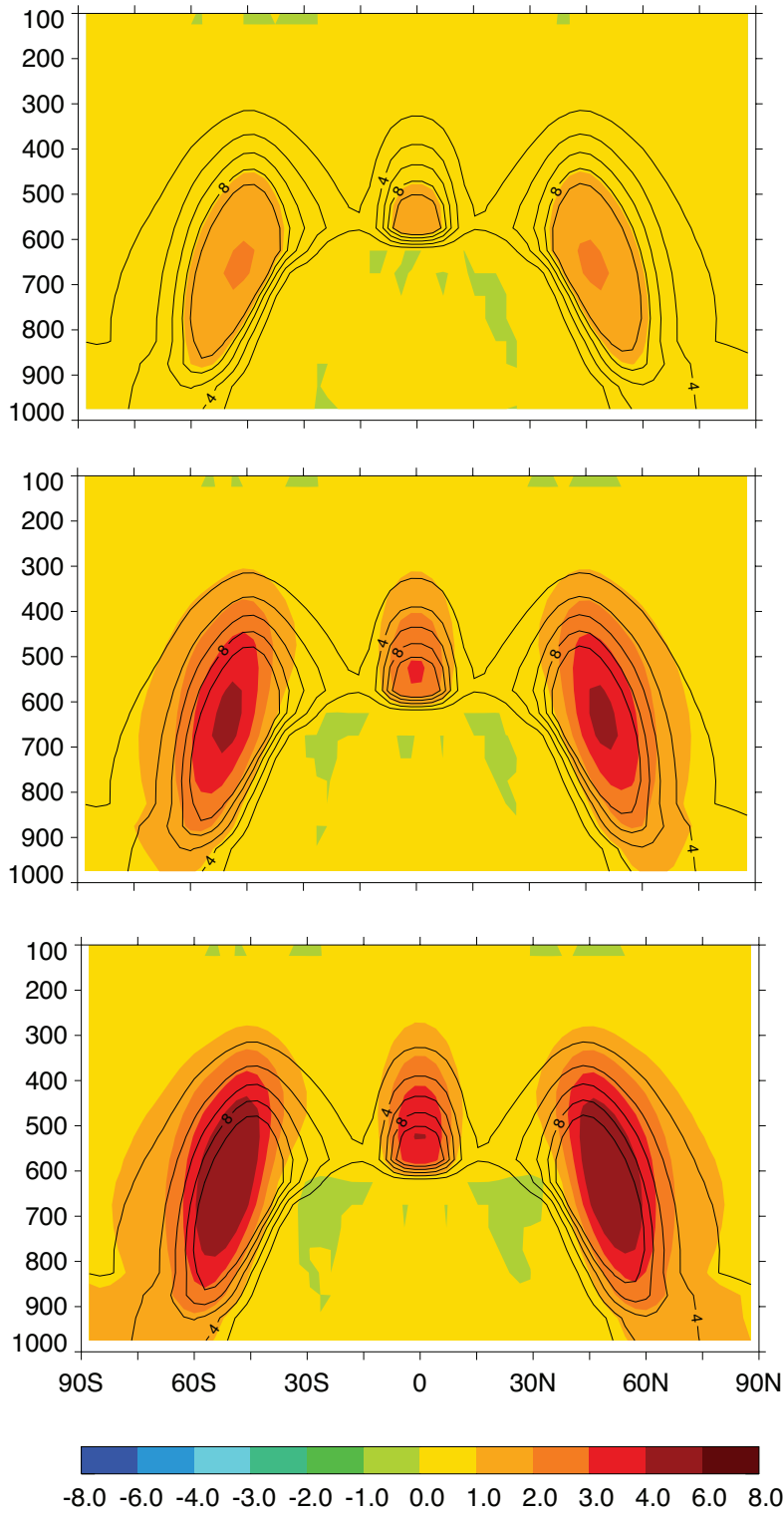


FIG. 11. Cloud ice difference ($10^{-6} \text{ kg kg}^{-1}$) between UN and CNTL-C (the upper panel), between TS and CNTL-C (the middle panel) and between TC and CNTL-C (the lower panel). The contours represent the cloud fraction in CNTL-C.