Moisture and moist static energy budgets of South Asian monsoon low pressure systems in GFDL AM4.0

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ABSTRACT

The mechanisms that lead to the propagation of anomalous precipitation in monsoon low 5 and high pressure systems, collectively referred to as synoptic-scale monsoonal disturbances 6 (SMDs), are investigated using daily output fields from GFDL's atmospheric general cir-7 culation model (AM4.0). On the basis of linear regression analysis of westard-propagating 8 rainfall anomalies of timescales shorter than 15 days, it is found that SMDs are organized 9 into wavetrains of 3-4 individual ciclones and anticyclones. These events amplify over the 10 Bay of Bengal, reach a maximum amplitude over the eastern coast of India and dissipate as 11 they approach the Arabian Sea. 12

It is also found that the precipitation anomalies in SMDs are highly correlated in 13 space with column-integrated water vapor. Based on this correlation, we analyze the col-14 umn moisture and frozen moist static energy (MSE) budgets as proxies for the propagation 15 of the precipitation anomalies. Propagation of the moisture anomalies is dominated by ver-16 tical moisture advection while the MSE anomalies propagate due to horizontal advection 17 of dry static energy by the anomalous winds. By combining the budgets, we interpret the 18 propagation of the precipitation anomalies in terms of lifting that is forced by horizontal 19 dry static energy advection, that is, ascent along sloping isentropes. This process moistens 20 the lower free-troposphere, producing an environment that is conducive to deep convection. 21 Longwave radiative heating is the main mechanism for maintaining MSE and precipitation 22 anomalies. 23

²⁴ 1. Introduction

The Indian summer monsoon features large spatial and temporal variations in pre-25 cipitation (Chang 2017). Among the transient disturbances that grow in these region are 26 synoptic-scale cyclones that are often referred to as monsoon low pressure systems. These 27 systems are characterized by slow westward and northward propagation and a horizontal ra-28 dius of ~ 2000 km (Godbole 1977; Krishnamurti and Chow 1975, 1976; Sikka 1977; Lau and 29 Lau 1990). The India Meteorological Department (IMD) categorizes monsoon low pressure 30 systems according to the strength of surface wind speed. The weakest systems are defined 31 as lows, stronger systems with surface winds between 8.5 and 16.5 m s⁻¹ are defined as mon-32 soon depressions, and the strongest systems are referred to as cyclonic storms (Saha et al. 33 1981; Krishnamurthy and Ajayamohan 2010; Hunt et al. 2016). Anomalous anticyclones are 34 also observed during the Indian monsoon, which have structures similar to the low pressure 35 systems but with reversed polarity (Krishnamurthy and Ajayamohan 2010). We will collec-36 tively refer to the high and low pressure systems as synoptic-scale monsoonal disturbances 37 (SMDs) (Krishnamurthy and Ajavamohan 2010; Ditchek et al. 2016). 38

During their lifecycle, monsoon low pressure systems often make landfall over the Indian subcontinent, producing up to half of the total monsoon rainfall received by India (Stano et al. 2002; Ding and Sikka 2006; Yoon and Chen 2005; Yoon and Huang 2012). Conversely, high pressure systems are associated with breaks in the monsoon, with little or no rainfall occurring during the passage of these systems. Thus, understanding SMDs is of critical importance to our understanding of the Indian monsoon and its variability.

In spite of the important role that SMDs have in the monsoon's hydrologic cycle, very few studies have analyzed how these systems modulate rainfall. Many studies have assumed that SMDs are a result of a variant of baroclinic instability called moist baroclinic instability (Salvekar et al. 1986; Krishnakumar et al. 1992; Krishnamurti et al. 2013, see also Cohen and Boos 2016 for a review on the topic), with precipitation being a result of largescale quasi-geostrophic (QG) ascent in these disturbances (Shukla 1978; Mak 1983; Sanders ⁵¹ 1984). Other studies have included moist convection in the form of frictional convergence
⁵² feedbacks (Goswami 1987).

To our best knowledge, the first study to examine the water vapor budget of SMDs 53 was Yoon and Chen (2005). They found that the leading balance in SMDs involves import of 54 moisture through convergence and loss of moisture through condensation and precipitation. 55 Their study, however, did not consider the Eulerian temporal tendency in moisture in the 56 budget, neglecting it under the assumption that it contributed little to the total budget. 57 However, recent studies have shown that SMDs are characterized by large moisture anomalies 58 (Krishnamurthy and Ajayamohan 2010; Hunt et al. 2016). The large amplitude of specific 59 humidity together with the ~ 5 day timescale of SMDs suggests that the temporal tendency 60 in moisture may not be negligible. Understanding the evolution of moisture, and the related 61 moist static energy (MSE), may lead to novel insights into the dynamics of SMDs. 62

The goal of this study is to analyze the moisture and MSE budgets of SMDs. To 63 carry out this analysis, we will make use of daily fields from GFDL's atmospheric general 64 circulation model (AGCM). We use this model because it captures the main features of 65 SMDs, and because it does not exhibit the large residuals in moisture/MSE budgets that 66 reanalysis products have as a result of the data assimilation process (Mapes and Bacmeister 67 2012). Additionally, previous studies have shown that models are able to simulate SMDs 68 reasonably well (Ashok et al. 2000; Sabre et al. 2000; Sø rland et al. 2016; Hunt and Turner 69 2017). We will show that the propagation of the moisture anomalies is dominated by vertical 70 moisture advection while propagation of the MSE anomalies is dominated by horizontal 71 MSE advection. While these two processes may seem distinct, we will show that horizontal 72 dry static energy advection can induce vertical motion, which in turns induces a moisture 73 tendency through vertical moisture advection. 74

This study is structured as follows. The next section describes AM4.0 and the methods of analysis. Section 3 describes the Indian monsoon mean state and variability as simulated by AM4. Section 4 and 5 discusses the moisture and moist static energy (MSE) ⁷⁸ budgets of SMDs, respectively. Section 6 synthesizes the results from the two budgets. A
⁷⁹ concluding discussion is offered in section 7.

⁸⁰ 2. Data and Methods

⁸¹ a. Model description

Most of the analysis presented here is made using daily output data from GFDL's 82 AGCM (AM4.0, Zhao et al. 2017a,b). AM4.0 uses a finite volume, cubed-sphere topology 83 with ~ 100 km resolution per cube face. The output resolution used here is on a $1.25^{\circ} \times 1^{\circ}$ 84 longitude-latitude grid. The model contains 33 vertical hybrid sigma-pressure levels (Sim-85 mons and Burridge 1981) extending from the surface to 1 hPa. Convection is parameterized 86 in terms of a double plume scheme, which is similar to the shallow convection scheme de-87 scribed in Bretherton et al. (2004) but extended to include an additional plume to represent 88 deep convection. Further details about the model configuration and its initial performance 89 have been documented by Zhao et al. (2017a,b). 90

The simulations here are made using prescribed present-day sea surface temperature boundary conditions (Zhao et al. 2017a). The experiments are run for one year as spinup, and then run for an additional 10 years. We analyze the last 10 years of the simulation. Because we are mainly interested in the dynamics of SMDs in this model, we restrict our analysis to the boreal summer months of June through September (JJAS).

The following AM4.0 fields are used in this study: the horizontal winds (u,v), geopotential height (Z), specific humidity (q), precipitation (P), dry static energy (s), frozen moist static energy (h), surface and top of the atmosphere shortwave (SW) and longwave (LW)radiative fluxes, and surface sensible H and latent heat fluxes E. In addition to daily data from AM4.0, two other datasets are used in this study. We make use of the $1.5^{\circ} \times 1.5^{\circ}$ horizontal resolution, daily geopotential height and wind data from the ERA-Interim (Dee et al. 2011) for the 33-year time period of 1979-2011. Rainfall data from the Tropical Rainfall Measurement Mission product 3B42 (TRMM-3B42, Huffman et al. 2007) is also used in this
 study.

105 b. Methods

Many of the results shown in the following sections are obtained through linear re-106 gression analysis, following the method described in Adames and Wallace (2014). We create 107 a time series that describes the evolution of SMDs over the Bay of Bengal. Daily precip-108 itation data, filtered to retain timescales shorter than 15 days and westward-propagating 109 zonal wavenumbers 3-25 using the method of Hayashi (1979), is used to create this index. 110 The filtered data was averaged over 85-90°E, 15-20°N, where monsoon low-pressure system 111 activity is strongest (Sikka 1977; Godbole 1977; Boos et al. 2015). This method is similar 112 to the method employed by Yoon and Chen (2005) and Chen et al. (2005). The statistical 113 significance of the regression patterns was tested via a two-tailed t-test, and the contour and 114 shading intervals are selected to roughly represent the 95% confidence interval. 115

In Section 3 we make use of space-time spectral analysis, following the methods of 116 Wheeler and Kiladis (1999) and Hendon and Wheeler (2008). In order to extract the signal 117 from SMDs, the time series of precipitation is divided into 60 day segments that overlap by 118 30 days. The segments are tapered to zero through the use of a Hanning window. We also 119 use a Hanning window in longitude to emphasize tropical wave activity occurring over the 120 longitude range of 50°-130°E. After tapering, complex fast Fourier transforms (FFTs) are 121 computed in longitude and then in time. Finally, the power spectrum is averaged over all 122 segments and over the $10^{\circ}-25^{\circ}N$ latitude belt. The number of degrees of freedom is calculated 123 to be 121 [2 (amplitude and phase) \times 10 (years) \times 365 \times (days)/60 (segment length)]. We 124 calculate the signal as $(P_{xx} - P_{red})/P_{xx}$, where P_{red} is the red spectrum, calculated using 125 Eq. (1) of Masunaga (2007), and a value of 0.5 is considered to be statistically significant in 126 this study. We have found the analysis to be insensitive to the length of the spatial Hanning 127 window, or the choice of segment length as long as the SMD activity is captured by the 128

129 spectral analysis.

In Sections 5 and 6 the moisture and frozen MSE budgets of SMDs are presented, 130 respectively. Some of these budget terms exhibit large residuals due to numerical errors in the 131 calculations of the budgets. These errors arise from the complex topography characteristic of 132 South Asia, from the calculation of numerical gradients and from the interpolation from the 133 model's native grid to the coordinate system used here. In order to reduce these residuals, we 134 apply the adjustment method described in the Appendix of Hill et al. (2017). This method 135 adds a barotropic adjustment to the horizontal wind field in order to satisfy conservation of 136 column-integrated moisture/MSE. Using this method largely reduces the residual from these 137 numerical errors. 138

Additionally, in Sections 5 and 6 we employ a compositing technique in space that 139 smooths out small-scale noise in the South Asian monsoon, so that the synoptic-scale struc-140 ture of the moisture and MSE budgets can be brought out more clearly. We will refer to 141 this technique as an SMD composite. In this procedure, we generate multiple maps by shift-142 ing the longitude-latitude box of the SMD index (85-90°E, 15-20°N) by up to two degrees 143 north/south and/or west/east. For example, regression maps are generated by using indices 144 centered on 85-90°E, 14-19°N, or 85-90°E, 16-21°N. Each of these maps is then shifted such 145 that the center of the moisture/MSE anomalies is centered over the 85-90°E, 15-20°N box. 146 The SMD composite is then obtained by averaging all of the regression maps. 147

¹⁴⁸ 3. Monsoonal mean state and variability in AM4

Figure 1 shows the JJAS mean 850 hPa geopotential height and horizontal winds for AM4.0 and ERA-Interim. AM4.0 captures the main features of the monsoonal circulation. The simulated monsoon trough is is situated over northeast India, with the corresponding increase in height southward towards the Indian Ocean. A low-level westerly jet is seen in the area where the height gradient is strongest. There are also some differences with respect

to ERA-Interim. AM4.0 exhibits stronger westerlies that extend further eastward past the 154 Philippines, and the geopotential height gradient is stronger. The difference in the westerly 155 jet is further shown in Fig. 2, along with moisture, precipitation and its variability. Mean 156 precipitation (panels a and b) in AM4.0, while of similar magnitude to TRMM, occurs at 157 different locations with respect to observations. While TRMM shows a rainfall maxima 158 along the western coast of India and over the northeastern Bay of Bengal, AM4.0 instead 159 exhibits a broader region of rainfall over northwest India that extends eastward and merges 160 with a second region of maximum rainfall that is centered over the Bay of Bengal. The 161 standard deviation of JJAS precipitation, shown in panel b, exhibits similar spatial patterns. 162 Additionally, it is clear that TRMM precipitation exhibits a larger variance than the model 163 does. This may be related to the inability of coarse-resolution GCMs to fully represent 164 the topographic features of South Asia, thus not adequately representing their effects on 165 precipitation. 166

Column-integrated water vapor, shown in Fig. 2c, exhibits horizontal pattern in 167 AM4.0 that is consistent with reanalysis, although AM4.0 slightly overestimates column 168 water in comparison to ERA-Interim. Column dry static energy, shown in panel (d), exhibits 169 slightly smaller values in AM4.0 than in ERA-Interim. Nonetheless, the two datasets exhibit 170 similar horizontal patterns, revealing that DSE increases with latitude during JJAS over 171 southern Asia. It will be shown in subsequent sections that this positive meridional DSE 172 gradient plays a central role in the propagation of the SMDs. Column MSE, shown in Fig. 173 2e is similar to column moisture, except the MSE maximum is shifted northward. 174

Figure 3a shows the JJAS signal strength of precipitation in AM4.0 averaged over the 10-25°N latitude belt. Variability in the South Asian monsoon region is dominated by westward-propagating synoptic-scale disturbances (zonal wavenumbers 3-25) with timescales between 3-15 days. This range of zonal and temporal scales is consistent with the documented scale of SMDs (Sikka 1977; Godbole 1977; Stano et al. 2002; Hunt et al. 2016). A weaker signal is also seen at eastward-propagating zonal wavenumbers 1-20 and timescales longer than 30 days, likely in association with the boreal summer intraseasonal oscillation (BSISO). In comparison, the signal strength for TRMM-3B42 rainfall, shown in Fig. 3b, is slightly weaker, but shows a nearly identical signal, with peak strength also occurring near zonal wavenumber 10 and 5-day timescales.

Based on the space-time variability in Fig. 3, we construct a SMD index by filtering 185 daily precipitation in order to retain westward-propagating zonal wavenumbers 3-25 and 186 timescales of 15 days and shorter (dashed box in Fig. 3). We have verified that our results are 187 robust to different choices of the filter as long as the frequencies and wavenumbers where SMD 188 activity is strongest is included (see Fig. 3). The filtered precipitation field is then averaged 189 over the 85-90°E, 15-20°N box. Regression maps of the horizontal structure of SMDs is shown 190 in Fig. 4. At lag day -2 an anticyclonic feature is seen over northeast India, with negative 191 precipitation anomalies centered near and to the west of the maximum height anomalies. 192 This anticyclone reaches a peak amplitude over India and dissipates as it reaches the Arabian 193 sea at lag day 1. The anomalous anticyclone is followed by a cyclonic anomaly coupled to 194 enhanced precipitation. The region of enhanced rainfall is first seen developing near the 195 coast of Myanmar at lag day -2. At lag day -1 the precipitation anomalies have amplified 196 and propagated west towards the Bay of Bengal. These anomalies are centered between 197 the minimum height anomalies and anomalous northerly flow, consistent with observations 198 (Warner 1984; Chen et al. 2005; Hunt et al. 2016), and other modeling studies (Ashok et al. 199 2000; Sabre et al. 2000; Hunt and Turner 2017). In subsequent days the region of enhanced 200 precipitation follows a pattern similar to the anticyclone that preceded it. The horizontal 201 structure and propagation of the depressions in Fig. 4 are similar to those seen in Fig. 2 of 202 Daggupaty and Sikka (1977) and Fig. 4 of Yoon and Chen (2005). 203

We can obtain some insights onto the vertical structure of the simulatd SMDs by analyzing longitude-height cross sections. Figure 5 shows a cross section of anomalous geopotential height Z', meridional winds v', vertical velocity ω' and specific humidity q overlaid by the meridionally-averaged zonal mass circulation ($\rho u', \rho w'$). Z' and v' are largely confined to the lower troposphere, with both exhibiting maximum amplitudes near the surface with little signature in the upper troposphere. ω' is a maximum in the mid-troposphere, exhibiting a structure reminiscent of a first baroclinic mode in vertical motion. q; is largely confined to the lowest levels of the troposphere, exhibiting a maximum between 850-900 hPa near 88°E and a minimum ~75°E and 650 hPa. Both q' and, to a lesser degree, v' exhibit westward tilt with height, possibly as a result of the low-level monsoon jet advecting the anomalies more strongly near the surface.

An interesting feature about the cross sections in Figs. 5a-b is the phasing between the fields. Both ω' and q' are shifted west of the region of low pressure, with ω' exhibiting a larger shift than q'. To further elucidate this phasing, Fig. 5c shows precipitation, column water vapor and vertical velocity averaged over the same latitudinal belt. Column water vapor and precipitation exhibit an in-phase relationship while mid-tropospheric ascent leads both fields by $\sim 5^{\circ}$ of longitude. All three fields are, in turn, shifted westward with respect to the center of the height anomalies.

Figure 6 shows a time-longitude diagram of anomalous precipitation associated with SMDs. It is clear from this diagram that the SMDs are arranged into a packet of 3-4 westward-propagating vortices. Each event propagates westward with a phase speed of \sim -4 m s^{-1} . The maximum amplitude of each event progressively shifts eastward, indicating that the wavetrain might be characterized by an eastward group velocity.

²²⁷ 4. Column-integrated moisture budget

In the previous section we analyzed the mean state and variability in the South Asian monsoon as simulated by AM4. Precipitation variability in this region is found to be dominated by synoptic-scale features that resemble SMDs. In this section, we will seek to understand the evolution of the precipitation anomalies in these systems by analyzing the evolution of column-integrated moisture. Figure 7a shows column integrated moisture and precipitation in a SMD composite. The two fields are spatially correlated, with enhanced precipitation located in regions of enhanced moisture and vice versa for regions of suppressed precipitation. The correlation is more clear in Fig. 8, which shows the two fields in a scatterplot. A robust correlation of 0.84 is observed further suggesting a strong coupling between the two fields. We can thus define the precipitation anomalies as proportional to $\langle q' \rangle$ divided by a convective moisture adjustment timescale: $P' = \langle q' \rangle / \tau_c$. Through linear least-squares fit we find that the two fields are related by a timescale of ~ 4.5 hours.

Based on the strong correlation between column moisture and precipitation in these depression systems, we invoke the anomalous column-integrated moisture budget to understand the temporal evolution of precipitation in these systems

$$\frac{\partial \langle q' \rangle}{\partial t} = -\langle \mathbf{V} \cdot \nabla q \rangle' - \left\langle \omega \frac{\partial q}{\partial p} \right\rangle' + E' - P' \tag{1}$$

where **V** is the horizontal wind field, ω is the pressure velocity, and E' is the anomalous surface evaporation. Angle brackets correspond to vertical integration from 1000 hPa to 100 hPa, and primed angle brackets correspond to the same integral but for 15 day highpass filtered fields.

The contribution of each term in Eq. (1) to the propagation of the moisture anomalies 247 is shown in Figs. 7 and 9. Precipitation (Fig. 7a) and vertical moisture advection (Fig. 7b) 248 are the dominant terms and largely cancel one another. The sum of the two terms (Fig. 249 9b), which we will refer as the column moist process, is $\sim 15\%$ as large as the individual 250 terms that compose it. It moistens the atmosphere in regions anomalous northerly flow, 251 and dries in regions of southerly flow. Column moist processes are largely in-phase with the 252 moisture tendency in Fig. 9a, although they do not exhibit the poleward tilt with longitude 253 that the column moisture tendency shows (panel a). This result indicates that ascent, which 254 was shown to be shifted westward of $\langle q' \rangle$ in Fig. 5, moistens the atmosphere prior to the 255 maximum in anomalous precipitation. The sum of all the budget terms yields a negligibly 256 small residual (not shown). 257

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In comparison, horizontal moisture advection is largely in-phase with the moisture

anomalies and acts to damp them, with an additional component that shifts the moisture
tendency poleward. Surface evaporation anomalies, shown in Fig 9c contributes little to the
propagation of the moisture anomalies, only exhibiting anomalies over the Bay of Bengal.

We can assess the relative importance of the terms in Eq. (1) to the maintenance and propagation of $\langle q' \rangle$ by comparing their projections upon the $\langle q' \rangle$ and its tendency, following the methods of Andersen and Kuang (2012); Arnold et al. (2013) and Adames et al. (2016)

$$S_m(F) = \frac{||F \cdot \langle q' \rangle||}{||\langle q' \rangle \cdot \langle q' \rangle||}$$
(2a)

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$$S_p(F) = \frac{||F \cdot \partial \langle q' \rangle / \partial t||}{||\partial \langle q' \rangle / \partial t \cdot \partial \langle q' \rangle / \partial t||}$$
(2b)

where F corresponds to the right-hand-side terms in Eq. (1). The contribution of each term to the propagation and maintenance of the moisture anomalies is shown in Fig. 10. It is clear that the propagation of the moisture anomalies is dominated by column moist processes, with little contribution from horizontal moisture advection and surface evaporation. Column processes imports moisture into the low-pressure system, maintaining the region of anomalous precipitation against dissipation from horizontal moisture advection.

²⁷² 5. Frozen moist static energy budget

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In the previous section we analyzed the column-integrated moisture budget in order to understand the propagation of the precipitation anomalies in SMDs. It was shown that the difference between vertical moisture advection and precipitation dominates the propagation and maintenance of the moisture anomalies. In this section, we will analyze the columnintegrated frozen MSE (denoted by h) budget. We define the frozen moist static energy as:

$$h = C_p T + g Z + L_v q - L_f q_i \tag{3}$$

where T is temperature, q_i is the ice mixing ratio, L_v is the latent energy of vaporization, L_f is the latent energy of fusion and C_p is the specific heat of dry air at constant pressure. ²⁸¹ The MSE budget takes the following form

$$\frac{\partial \langle h' \rangle}{\partial t} \simeq -\langle \mathbf{V} \cdot \nabla h \rangle' - \left\langle \omega \frac{\partial h}{\partial p} \right\rangle' + \langle LW' \rangle + \langle SW' \rangle + H' + L_v E' \tag{4}$$

where LW' and SW' are the longwave and shortwave radiative heating anomalies, respectively and H' is the surface sensible heat flux. Note that the left-hand-side can be more accurately described by the sum of internal energy and potential energy (Hill et al. 2017), and h is commonly used as an approximation.

The column frozen MSE anomalies along with their tendency are shown in Fig. 9f. The $\langle h \rangle$ anomalies are broadly similar to the $\langle q \rangle$ anomalies shown in the left column, indicating that $\langle h \rangle$ is dominated by the contribution from moisture. $\partial \langle h' \rangle / \partial t$ also exhibits a similar horizontal pattern to $\partial \langle q' \rangle / \partial t$.

The leading terms in the $\langle h' \rangle$ budget are shown in the right column of Fig. 9. The 290 largest contribution to the propagation of $\langle h' \rangle$ is horizontal MSE advection. This pattern 291 differs significantly than that of horizontal moisture advection in Fig. 9b, indicating that is 292 dominated by the advection of dry static energy (DSE). Instead, horizontal MSE advection 293 nearly matches the pattern of $\partial \langle h' \rangle / \partial t$ and is similar to the spatial pattern of the column 294 moisture process. Vertical MSE advection acts to offset horizontal MSE advection but it 295 is also shifted slightly eastward, acting to damp the MSE anomalies. Anomalous longwave 296 radiative heating, while exhibiting smaller amplitude, is largely in phase with the MSE 297 anomalies. 298

The results shown in Fig. 9 indicate that horizontal DSE advection is key to the propagation of the MSE anomalies. To further elucidate the physical processes that dominate horizontal MSE advection, we separate it into contribution arising from interactions from different temporal scales, following the methods of Maloney (2009); Kiranmayi and Maloney (2011) and Adames et al. (2016):

$$-\langle \mathbf{V} \cdot \nabla h \rangle' \simeq -\langle \mathbf{V}' \cdot \nabla \overline{h} \rangle' - \langle \overline{\mathbf{V}} \cdot \nabla h' \rangle' - \langle \mathbf{V}' \cdot \nabla h' \rangle'$$
(5)

³⁰⁴ where overbars denote 15-day lowpass filtered data. The terms on the right-hand side of

Eq. (5) correspond to horizontal advection of low-frequency MSE by the high-frequency 305 winds, horizontal advection of high-frequency MSE by the low-frequency winds, and the 306 nonlinear advection of anomalous MSE by the anomalous winds. The contribution of each 307 term to horiozntal MSE advection is shown in Fig. 11. It is clear that horizontal advection 308 of low-frequency MSE by the high-frequency winds dominates, and explains the majority of 309 the MSE tendency. The other two terms are small, and only contribute to shift the MSE 310 tendency northward. The sum of the three terms approximately captures the total horizontal 311 MSE advection shown in Fig. 9g. Since horizontal MSE advection is dominated by the DSE 312 component, this result implies that advection of the mean DSE in Fig. 2d by the anomalous 313 winds is the largest contributor to horizontal MSE advection. 314

The contribution of each term to the propagation and maintenance of MSE is shown in Fig. 10b. It is clear that horizontal MSE advection is the largest contributor to the propagation of the MSE anomalies, with some offset from vertical MSE advection. Longwave radiative heating maintains MSE against vertical MSE advection.

³¹⁹ 6. Bridging the budgets

In Sections 4 and 5 we analyzed the column moisture and moist static energy bud-320 gets, respectively, to understand the propagation of anomalous precipitation in SMDs. We 321 found that the difference between vertical moisture advection and precipitation dominates 322 the propagation of the moisture anomalies, while horizontal DSE advection dominates the 323 propagation of the MSE anomalies. In this section we will show how these two processes are 324 physically related. The column temperature trend in the simulated SMDs are $\sim 8\%$ as large 325 as the column apparent heating (not shown). If we neglect the temperature tendency in the 326 thermodynamic energy equation, the leading balance occurs between horizontal temperature 327 advection, vertical DSE advection and apparent heating. We may write this balance in terms 328

of the dry static energy budget with little loss of accuracy, as described by Sobel et al. (2014)

$$\left(\omega \frac{\partial s}{\partial p}\right)' \simeq -(\mathbf{V} \cdot \nabla s)' + Q_c' + Q_r' \tag{6}$$

where Q'_c and Q'_r are the convective and radiative contributions to apparent heating. Following the method of Chikira (2014) and Adames (2017), we can separate the pressure velocity term into three contributions, one from horizontal DSE advection, one from radiative heating and one from convective heating $\omega \simeq \omega_a + \omega_r + \omega_c$. If we assume that perturbations in the vertical DSE gradient are much smaller than those of the background DSE gradient, we can obtain the following

$$\omega_a' \simeq -(\partial \overline{s}/\partial p)^{-1} (\mathbf{V} \cdot \nabla s)' \tag{7a}$$

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$$\omega_c' \simeq (\partial \overline{s} / \partial p)^{-1} Q_c' \tag{7b}$$

$$\omega_r' \simeq (\partial \bar{s} / \partial p)^{-1} Q_r' \tag{7c}$$

where the overbar refers to timescales longer than 15 days. Note that ω'_a is adiabaticallydriven while $\omega'_c + \omega'_r$ is diabatically-driven.

By combining Eq. (1) and (7) it becomes clear that vertical moisture advection is 340 composed by a component that is driven by apparent heating, and an additional contri-341 bution that is forced by horizontal DSE advection. The former implies vertical motion in 342 regions of apparent heating while the latter implies ascent in regions of positive DSE ad-343 vection (i.e. warm air advection). Thus, ω'_a is related to ascent that occurs as air parcels 344 move along sloping isentropic surfaces (isentropic ascent). The contribution of isentropic 345 ascent and diabatic heating to total vertical motion is shown in Fig. 12a. Ascent driven by 346 diabatic heating is the dominant term and predominantly contributes to the maintenance of 347 the moisture anomalies. Ascent driven by positive DSE advection is smaller in magnitude 348 and is responsible for shifting the vertical velocity anomalies west of the region of maximum 349 precipitation. A small residual exists, likely due to errors in the analysis and vertical mo-350 tion driven by nonlinear terms. It is clear from Fig. 12b that ω'_a is largely in phase with 351

 $\partial \langle q' \rangle \partial t$, with a spatial correlation of ~0.9 (not shown). Thus ω'_a predominantly contributes to propagation of the SMDs by advecting moisture vertically in regions of isentropic ascent:

$$\frac{\partial \langle q' \rangle}{\partial t} \sim -\left\langle \omega_a' \frac{\partial \overline{q}}{\partial p} \right\rangle \tag{8}$$

Thus, that horizontal MSE advection dominates the propagation of the MSE anomalies is consistent with column processes dominating the propagation of the moisture anomalies. Equation (8) is a departure from the typical assumptions made for SMDs, where the quasigeostrophic (QG) omega equation (See Eq. 6.34 in Holton 2004) is used to diagnose precipitation ($P' \propto \omega'_a$) and moisture tendencies are ignored (Rao and Rajamani 1970; Sanders 1984; Chen et al. 2005).

Similarly, anomalous radiative heating induces vertical motion that acts to maintain the anomalous precipitation in SMDs. Thus, that radiative heating maintains the MSE anomalies is consistent with column processes dominating the maintenance of the moisture anomalies.

³⁶⁴ 7. Concluding Discussion

In this study we analyzed the column moisture and MSE budgets of synoptic-scale 365 monsoon disturbances (SMDs) as simulated by GFDL's AM4.0. AM4.0 captures a mean 366 JJAS flow and horizontal distributions of moisture, DSE and MSE that are consistent with 367 those of ERA-Interim. However, the model fails to accurately describe the distribution 368 of climatological-mean precipitation. In spite of this caveat, the model captures SMDs 369 that are consistent with observations (Daggupaty and Sikka 1977; Chen et al. 2005). This 370 result suggests that SMDs might not be sensitive to the details of the climatological-mean 371 distribution of precipitation. 372

The simulated SMDs are found to exhibit a life cycle where they develop over the Bay of Bengal, attain a maximum amplitude as they make landfall over India and then dissipate as they reach the Arabian Sea. A lag regression analysis reveals that these systems are arranged into wavetrains of 3-4 events that propagate westward.

The processes that maintain and propagate these SMDs are analyzed on the basis of 377 column-integrated moisture and MSE budgets. In the moisture budget, it is found that the 378 sum of vertical moisture advection and precipitation (column processes) dominates both the 379 propagation and maintenance of the low-pressure system. This moisture tendency results 380 from anomalous vertical moisture advection slightly leading the precipitation anomalies as 381 the SMD propagates westward, indicating that vertical moisture advection from deep ascent 382 moistens the atmosphere prior to the maximum in anomalous precipitation. Similarly, verti-383 cal moisture advection maintains the precipitation anomalies against damping by horizontal 384 advection. 385

The column MSE budget reveals that the processes that maintain the SMDs differ 386 from those that induce its propagation. Horizontal MSE advection dominates the propa-387 gation of the MSE anomalies. Because the horizontal structure of MSE advection differs 388 from that of horizontal moisture advection, it can be inferred that it is dominated by the 389 DSE component. When both MSE and moisture budgets are considered together, and by 390 assuming that the column-integrated temperature tendency in these disturbances is negli-391 gible, it is found that horizontal DSE advection induces vertical motion. This ascent, in 392 turn, moistens the atmosphere to the west of the maximum precipitation anomalies. Ascent 393 driven by horizontal DSE advection corresponds to lifting ocurring along isentropic surfaces. 394

In contrast, it is found that longwave radiative heating maintains the MSE anomalies against dissipation from horizontal moisture advection. This anomalous heating induces vertical motion which supplies the precipitation anomalies with additional water vapor. The same mechanism is suggested to play a key role in the maintenance of the MJO (Andersen and Kuang 2012; Chikira 2014; Sobel et al. 2014; Wolding et al. 2016) and in convective self-aggregation (Bretherton et al. 2005; Wing and Emanuel 2014).

401 Many studies have used the quasi-geostrophic (QG) approximation to analyze the 402 propagation of monsoon depressions, using the QG omega equation to diagnose the region of

anomalous precipitation (Mak 1982; Sanders 1984). However, we found that vertical motion 403 is not directly related to precipitation. Instead, it is column moisture that is spatially 404 correlated to precipitation, and vertical motion is found to be more closely related to the 405 moisture tendency. This is a large departure from QG theory. This departure is important as 406 it indicates that QG cannot account for the evolution of convection in these systems. Instead, 407 vertical motion, water vapor and precipitation interact with each other, with isentropic lift 408 acting increase column water vapor, which in turn produces a thermodynamic environment 409 that favors increased precipitation. 410

There are a few limitations to this study. While moisture is the largest contributor 411 to MSE, it only accounts for $\sim 75\%$ of the total vertically-integrated MSE (not shown). 412 Thus, DSE accounts for roughly a quarter of the total frozen MSE, a non-negligible amount. 413 Thus, the approximations shown in Section 6, while informative, are only qualitative. A 414 rigorous, vertically-resolved analysis of moisture, ice and other thermodynamic variables 415 could further elucidate the mechanisms that drive SMDs. Nonetheless, the results presented 416 in this study indicate that analyzing moisture and MSE budgets provide useful insights on the 417 structure and propagation of SMDs. Furthermore, incorporating these equations into a linear 418 theoretical framework for monsoon depressions may also shed light on our understanding of 419 these systems. Such a framework is presented in a companion paper. 420

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⁶⁵⁸ 8 Scatterplot of anomalous column integrated water vapor $\langle q' \rangle$ and precipitation ⁶⁵⁹ P' from all points within 10-25°N, 60-100°E domain in the regression maps ⁶⁶⁰ that make up the SMD composite. The linear least squares fit line is shown ⁶⁶¹ in thick black. The slope of the linear fit is shown, in units of days, in the top ⁶⁶² left along with the linear correlation coefficient.

- 9 SMD composite of the column-integrated moisture (left) and MSE (right) 663 budgets. Panels (a)-(d) show column moisture as the contoured field and (a)664 the moisture tendency, (b) sum of vertical moisture advection and precipita-665 tion, (c) horizontal moisture advection and (d) surface latent heat fluxes as 666 shaded fields. Panels (e)-(h) show column MSE as the contoured field (e) the 667 column MSE tendency (f) Vertical MSE advection, (g) horizontal MSE ad-668 vection, (h) longwave radiative heating as shading. Shading is in units of W 669 m⁻². Contour interval 0.25×10^6 J m⁻². The 850 hPa anomalous horizontal 670 winds is shown as arrows in all panels. 671
- 10 Normalized contribution of the individual terms in the column-integrated 672 moisture (a) and MSE budgets (b) to the maintenance (top) and propaga-673 tion (bottom) of the regressed SMDs. The terms are obtained by projecting 674 $\langle q' \rangle$ and $\langle h' \rangle$ (top panel) and $\partial \langle q' \rangle / \partial t$ and $\partial \langle h' \rangle / \partial t$ (bottom) onto the individ-675 ual contributions to the moisture/MSE budget using Eq. (2). The terms of 676 the moisture budget are (from left to right) horizontal moisture advection, the 677 sum of vertical moisture advection and precipitation, surface evaporation, the 678 residual after adding all terms, and the moisture tendency. The MSE budget 679 terms are (from left to right) horizontal MSE advection, vertical MSE advec-680 tion, longwave radiative heating, shortwave radiative heating, surface latent 681 heat fluxes, surface sensible heat fluxes, the residual and the MSE tendency. 682

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FIG. 1. Mean JJAS geopotential height (shading) and horizontal flow (arrows) for AM4.0 (top) and ERA-Interim (bottom). The longest arrows correspond to winds of $\sim 15 \text{ m s}^{-1}$. Blank shading in the top panel corresponds to regions where the Z field is beneath the surface.



FIG. 2. Mean JJAS zonal wind (contours) and (a) mean JJAS precipitation, (b) standard deviation of JJAS precipitation, (c) JJAS column-integrated water vapor $\langle q \rangle$, (d) column DSE and (e) column MSE for (left) AM4.0 and (right) ERA-Interim/TRMM. Contour interval 2.5 m s⁻¹. Panels (d) and (e) are scaled by a factor of 10⁸.



FIG. 3. Signal strength of (a) AM4.0 and (b) TRMM-3B42 precipitation. The signal was obtained from data around the 10-25°N latitude belt, and longitudinally tapered to emphasize the Asian monsoon region over 50-150°E. The dashed lines highlight the box used to define the filter used to analyze SMDs in this study.



FIG. 4. Five panel sequence of AM4.0 anomalous precipitation (shading), 850 hPa Z' (contoured) and the anomalous horizontal winds (arrows) regressed onto precipitation data filtered to retain timescales shorter than 15 days and westward-propagating zonal wavenumbers 3-25, averaged over 15-20°N and 85-90°E. Each panel corresponds to lag regression at days -2,-1,0,1,2. The contour interval is 1.5 m.



FIG. 5. Longitude-height cross section of a monsoon low-pressure system averaged over the 10-25°N latitude belt. (a) Meridional wind (shading) and geopotential height (contoured) anomalies. Contour interval is 1.5 m. (b) Specific humidity q (shading) and vertical velocity (contours). Contour interval is 5 hPa day⁻¹. The largest zonal flux vector is about 0.5 kg m⁻² s⁻¹, and the largest vertical flux vector is about 0.001 kg m⁻² s⁻¹. Panel (c) shows anomalous column-averaged vertical velocity, precipitation and column water vapor averaged over the 10-25°N latitude belt. The fields have been normalized by their standard deviation to facilitate comparison.



FIG. 6. Time-longitude diagram of anomalous precipitation obtained from a lag regression of the SMD index described in Section 2. The fields have been averaged over the 10-25°N latitude belt. Contour interval 0.2 mm day⁻¹. The dotted lines are lines of constant speeds of -4 m s^{-1} and 2 m s⁻¹.



FIG. 7. SMD composite of anomalous column-integrated water vapor (contours) and anomalous precipitation (shading in a) and column-integrated vertical moisture advection (shading in b). Contour interval 0.25×10^6 J m⁻². The SMD composite is constructed by generating multiple regression maps from SMD indices that are slightly shifted in space (see Section 2b). Each of these maps is then shifted such that the center of the moisture/MSE anomalies is centered over the 85-90°E, 15-20°N box. The SMD composite is an average of all the regression maps. The terms are multiplied by $L_v = 2.5 \times 10^6$ J kg⁻¹ to facilitate comparison with the MSE budget. The 850 hPa anomalous horizontal winds is shown as arrows in both panels.



FIG. 8. Scatterplot of anomalous column integrated water vapor $\langle q' \rangle$ and precipitation P' from all points within 10-25°N, 60-100°E domain in the regression maps that make up the SMD composite. The linear least squares fit line is shown in thick black. The slope of the linear fit is shown, in units of days, in the top left along with the linear correlation coefficient.



FIG. 9. SMD composite of the column-integrated moisture (left) and MSE (right) budgets. Panels (a)-(d) show column moisture as the contoured field and (a) the moisture tendency, (b) sum of vertical moisture advection and precipitation, (c) horizontal moisture advection and (d) surface latent heat fluxes as shaded fields. Panels (e)-(h) show column MSE as the contoured field (e) the column MSE tendency (f) Vertical MSE advection, (g) horizontal MSE advection, (h) longwave radiative heating as shading. Shading is in units of W m⁻². Contour interval 0.25×10^6 J m⁻². The 850 hPa anomalous horizontal winds is shown as arrows in all panels.



FIG. 10. Normalized contribution of the individual terms in the column-integrated moisture (a) and MSE budgets (b) to the maintenance (top) and propagation (bottom) of the regressed SMDs. The terms are obtained by projecting $\langle q' \rangle$ and $\langle h' \rangle$ (top panel) and $\partial \langle q' \rangle / \partial t$ and $\partial \langle h' \rangle / \partial t$ (bottom) onto the individual contributions to the moisture/MSE budget using Eq. (2). The terms of the moisture budget are (from left to right) horizontal moisture advection, the sum of vertical moisture advection and precipitation, surface evaporation, the residual after adding all terms, and the moisture tendency. The MSE budget terms are (from left to right) horizontal MSE advection, vertical MSE advection, longwave radiative heating, shortwave radiative heating, surface latent heat fluxes, surface sensible heat fluxes, the residual and the MSE tendency.



FIG. 11. As in Fig. 9 but the shaded fields show (a) horizontal advection of low-frequency MSE by the high-frequency winds, (b) horizontal advection of high-frequency MSE by the low-frequency winds, (c) horizontal advection of high-frequency MSE advection by the high-frequency winds and (d) the sum of (a)-(c). The 850 hPa anomalous horizontal winds is shown as arrows.



FIG. 12. (a) As in Fig. 5c but showing column-averaged $-\omega$ as a solid line, $-\omega'_a$ in red, $\omega'_c + \omega'_r$ in blue, and the residual $\omega' - \omega'_a - \omega'_c - \omega'_r$ as a dotted line. (b) Column-integrated vertical moisture advection by ω'_a (red solid) and $\partial \langle q' \rangle / \partial t$ (dotted line).