

A microscopic view of radiolarians, which are single-celled organisms that produce intricate, spherical shells made of silica. The shells are composed of numerous thin, radiating spines that form a star-like or spherical pattern. The organisms are shown in various orientations and sizes against a dark, slightly textured background.

# Fisheries and ecosystems

**Princeton,  
June, 2009**

# The Roots of Mathematical Ecology were in Marine Ecosystems

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**Vito Volterra**

(1860-1940)

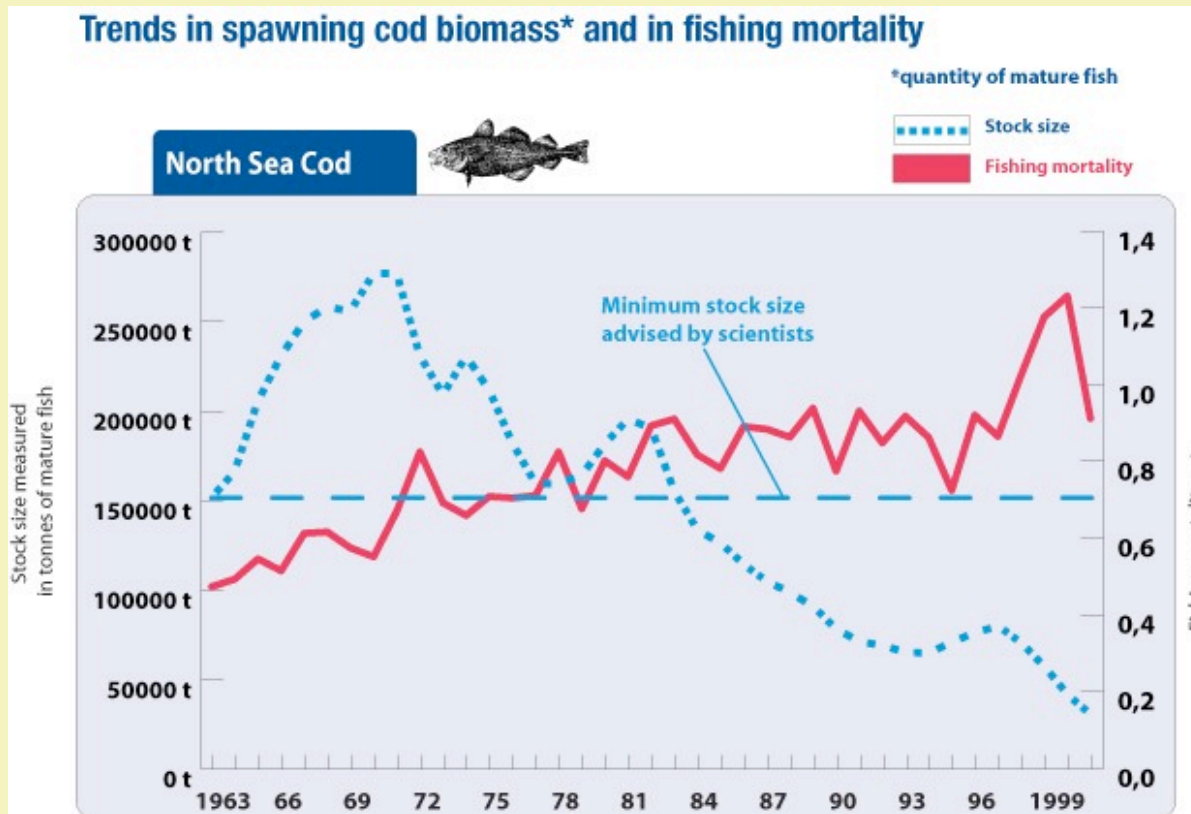
Volterra was enticed by his son-in-law,  
Umberto D'Ancona, to explain the  
fluctuations in the Adriatic Fisheries





Vito Volterra

# Despite this elegant theory, marine management has been a disaster





*Vito Volterra*

Despite elegant theory, we have not sustained these resources

- Marine ecosystems are complex systems, characterized by nonlinearities and sudden flips





Despite elegant theory, we have not sustained these resources

- They are **complex adaptive systems**, integrating phenomena at multiple scales



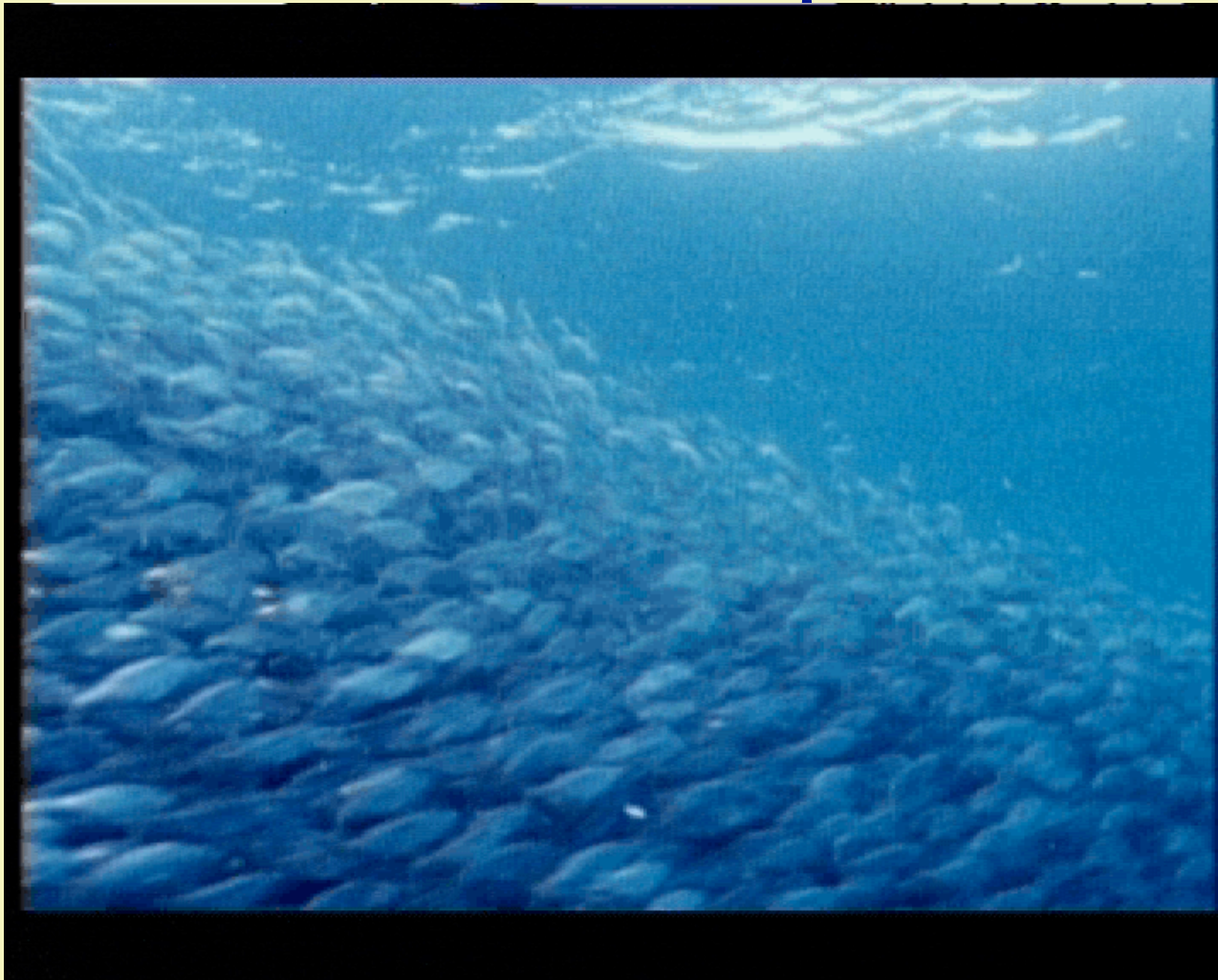
This implies a need to relate phenomena across scales, from

- Cells and nutrients to organisms to collectives to ecosystems, N-P-Z-F

*and to ask*

- How robust are the properties of ecosystems?
- How does the answer to this vary as a function of scale -- spatial, temporal, and organizational?
- How does robustness of macroscopic properties relate to ecological and evolutionary dynamics on finer scales?

# Scaling from microscopic to macroscopic



Iain Couzin, BBC



# Lagrangian-Eulerian connections



- **Begin from microscopic (Lagrangian) rules**

$$m\ddot{x} = F_1 + F_2 + F_3 + F_4$$

Random      Directed      Grouping      Arrayal



## Flierl et al.: Boltzmann equation

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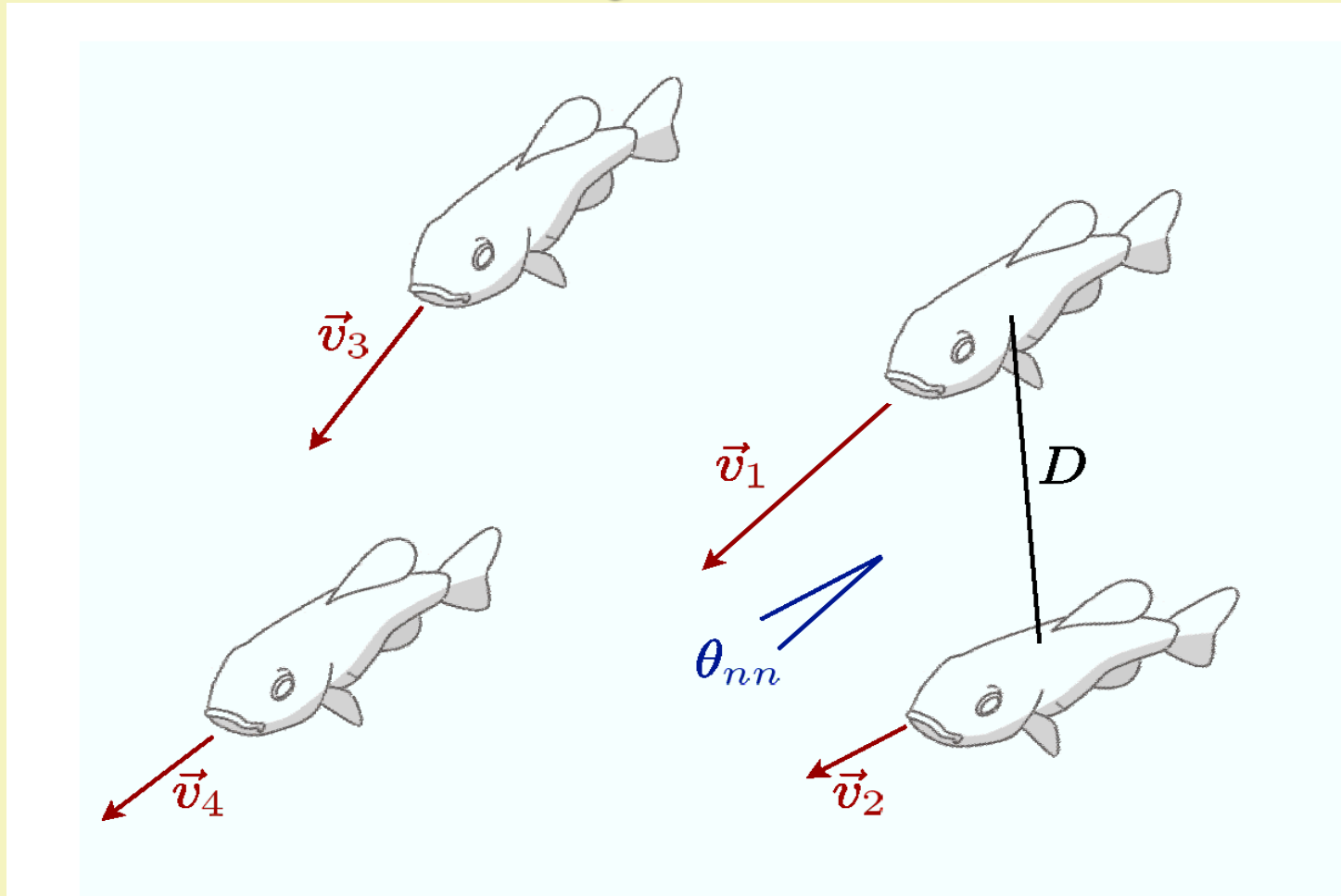
$$\begin{aligned} \frac{\partial}{\partial t} n(x, v, t) = & - \frac{\partial}{\partial x_i} [v_i n(x, v, t)] \\ & - \frac{\partial}{\partial v_i} [a_i n(x, v, t)] \\ & + \frac{1}{2} \frac{\partial^2}{\partial v_i \partial v_j} [\gamma_{ij} n(x, v, t)]. \end{aligned}$$

# Couzin, Krause, Franks, Levin



- Utilize simulations to explore these issues

# Velocity vectors

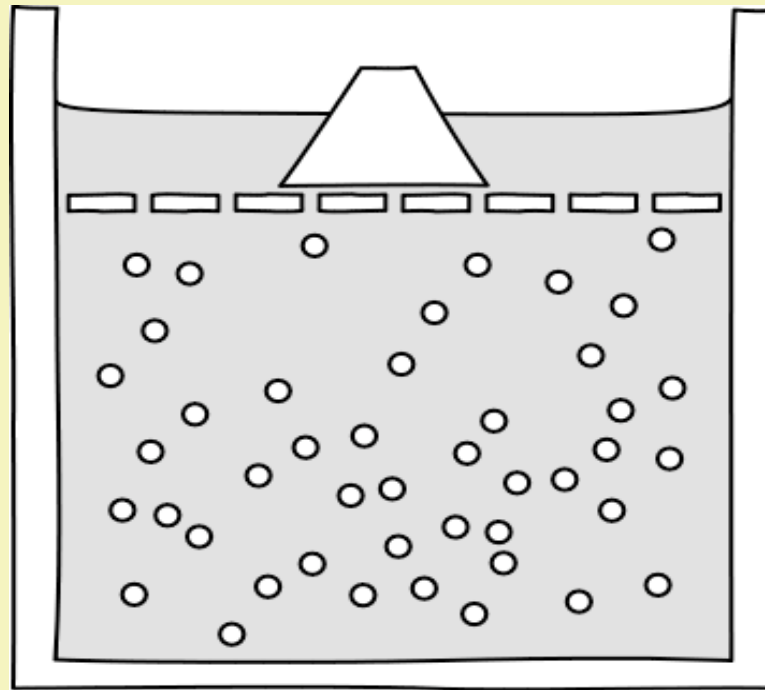


QuickTime™ and a  
decompressor  
are needed to see this picture.

There are striking regularities in macroscopic patterns, which support fisheries and other ecosystem services

- Element ratios
- Patterns of productivity
- Size-structure distributions

*Sustainability of fisheries and other ecosystem services* must focus on macroscopic features, while recognizing that control of those rests at lower levels of organization



Models too large, too complicated,  
too detailed should raise eyebrows





# Research challenges

- **Werner: Too much detail not necessarily a good thing**
- **Need to identify how to cluster**
- **Are there relevant functional groups, etc.?**
- **Can an evolutionary perspective guide aggregation?**

# Research challenges

- Identification of invariants and scaling laws, like the Redfield ratios
- Establishment of patterns of variation: Are they invariants?
- Development of theory to explain patterns, and that have predictive value

# Redfield ratios

(in marine organic matter)

P : N : C :  $-O_2$

(oxygen required to respire marine organic matter)

1 : 16 : 106 : 138

(subject to some debate)

# SINGLE-SPECIES/RESOURCE DYNAMICS

Klausmeier et al.

$$\begin{array}{l} \text{Ambient} \left\{ \begin{array}{l} \frac{dP}{dt} = a(P_{in} - P) - f_P(P)B \\ \frac{dN}{dt} = a(N_{in} - N) - f_N(N)B \end{array} \right. \\ \\ \text{Storage} \left\{ \begin{array}{l} \frac{dP_s}{dt} = Bf_P(P) - A\alpha B - mP_s \\ \frac{dN_s}{dt} = Bf_N(N) - A\beta B - mN_s \end{array} \right. \\ \\ \text{Biomass} \left\{ \begin{array}{l} \frac{dB}{dt} = AB - mB \end{array} \right. \end{array}$$

where

$$A = \mu \min(P_s / (P_s + \alpha B), N_s / (N_s + \beta B))$$

# **Klausmeier et al.:**

## **The evolutionary ecology of nutrient utilization**

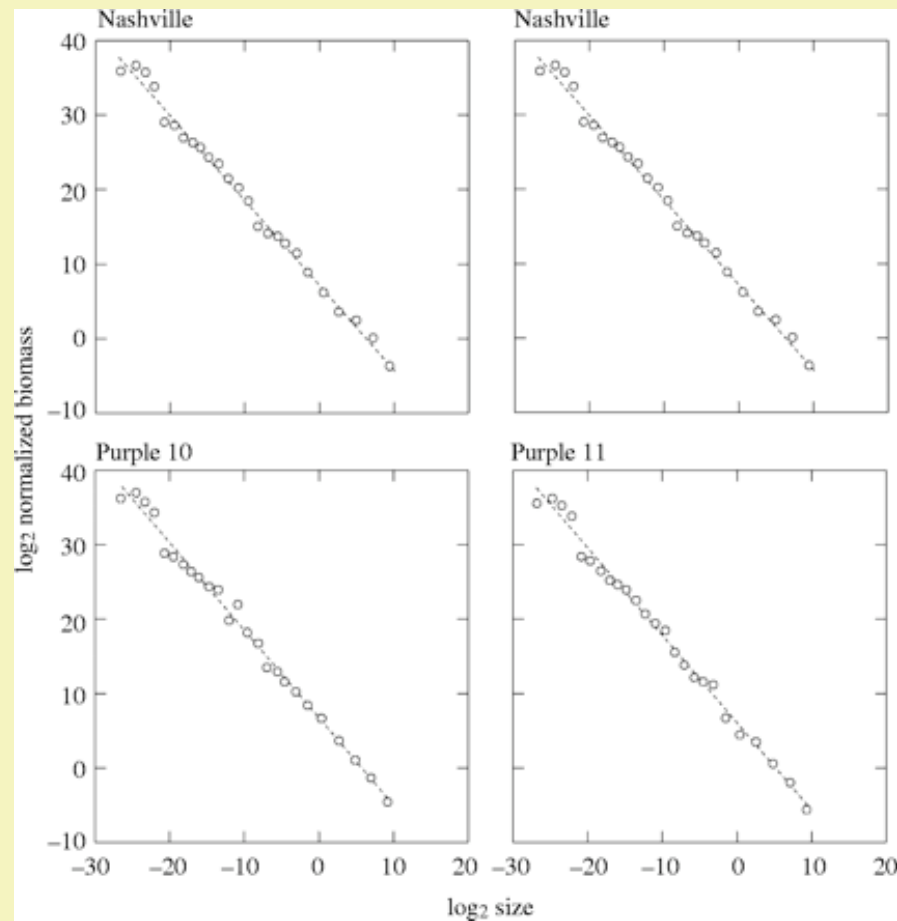
- Trait-dependent dynamics on ecological time scales
- Competition dynamics on evolutionary time scales

In a game-theoretic sense, what strategies are most successful at resource acquisition?

# Stoichiometry provides just one set of robust patterns



# Particle Size Spectrum (Sheldon)



Normalized biomass size-spectra in carbon units from several stations in the New England Seamounts Area (Northwest Atlantic). (Marquet et al, after Quiñones et al., 2003.)

# Oscar Schofield

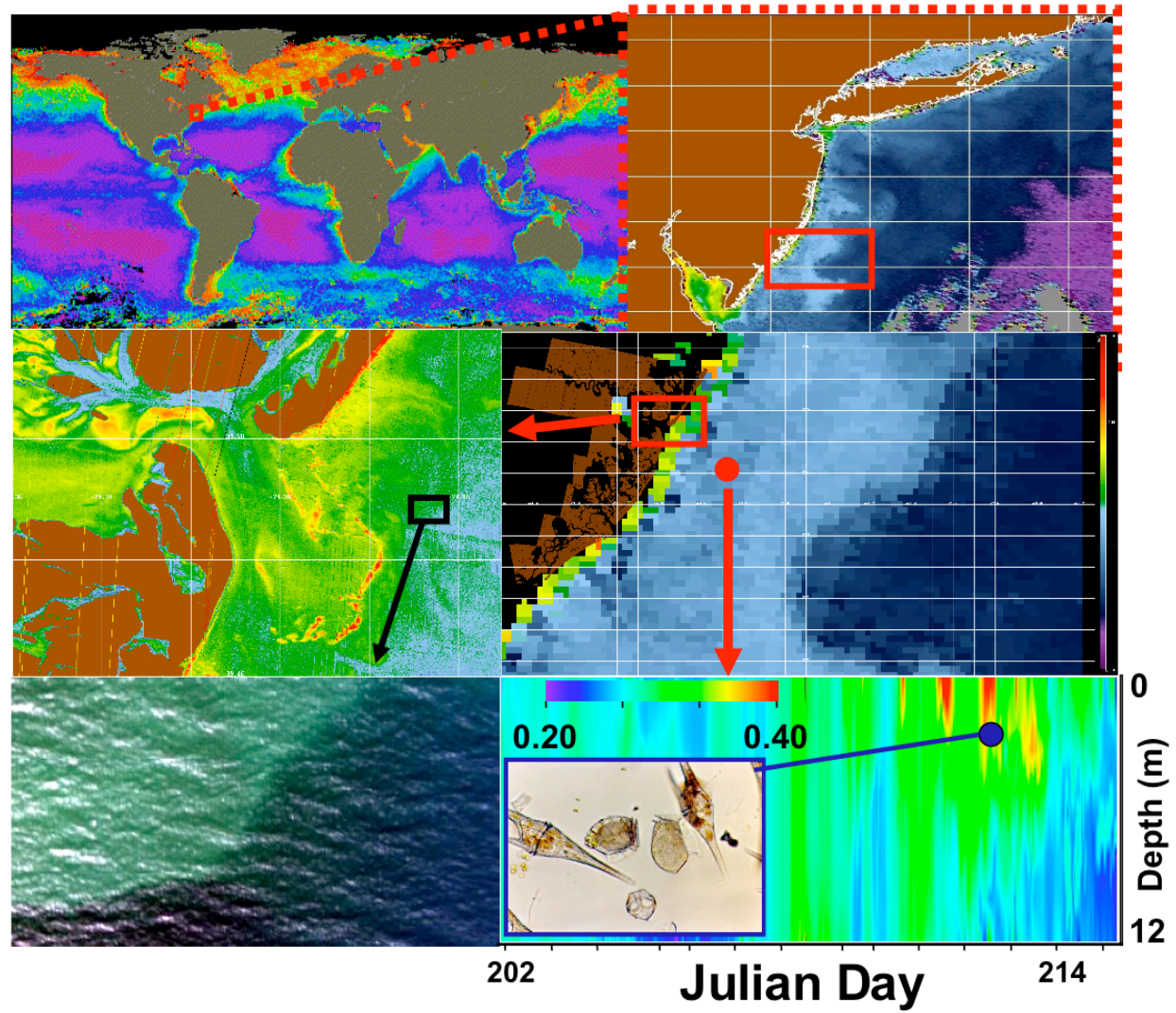


Figure 1: Variability in chlorophyll a over a range of scales.



# Goal of our work

- Characterize macroscopic patterns that maintain ecosystem properties, and support fisheries
- Develop models that explain those patterns
- Develop evolutionary models that allow prediction of what should be where, in relation to environmental conditions